

## The 28th International Energy and Environment Conference

# Performance analysis of mixed fuels in low and medium-temperature SOFC

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**Date: 08-10 September 2025**

Heart of the Beskid Mountains

Hydrogen and Fuel Cell Laboratory  
氫能與燃料電池實驗室

## Industry

Kaohsiung is the third most populated city in Taiwan with **2.77 million residents**. The City has transformed from an industrial center with refining and shipbuilding industries to focus on the semiconductor/ photoelectric, digital content, biomedical, cultural creativity, and tourism industries.



# Kaohsiung City



Source: Kaohsiung City Government

## Transportation

Kaohsiung is easily accessible by the **international airport (KHH)**, **high speed rail (THSR)**, TRA train, metro-rapid transit (KMRT), light rail (LRT), and Kaohsiung i-bus.

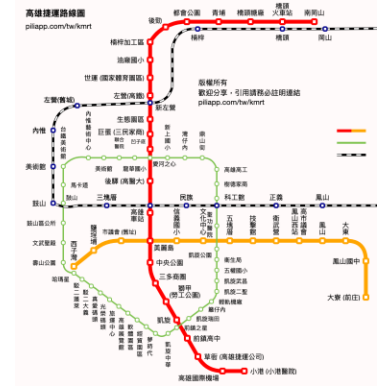


tw.myblog.yahoo.com/vanderson-travel

## Climate

Kaohsiung has tropical monsoon climate with an average temperature of 25°C, with high of 35°C in July and low of 10°C in January. Rain and typhoon usually occur in the summer months of June - August.

## Light Tail (LRT)



Source: Kaohsiung City Government



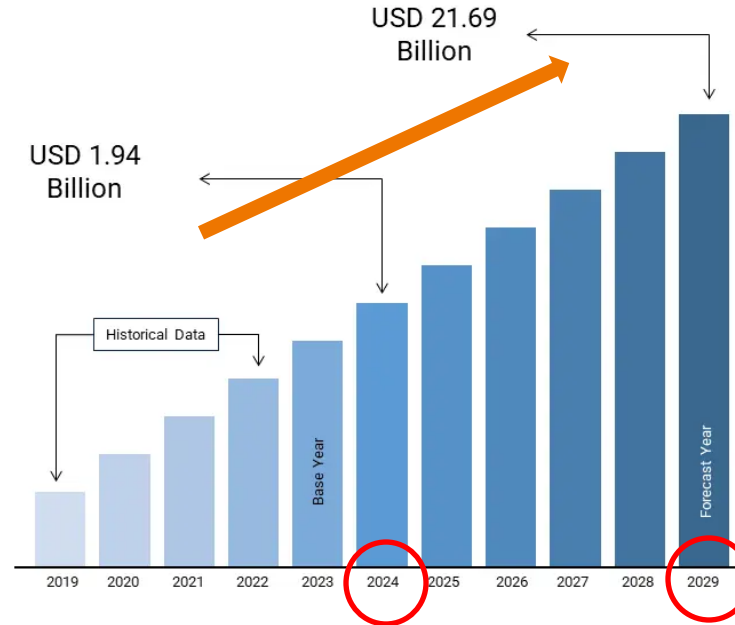
**Green Hydrogen Market** Expected to Experience **Robust Growth** with a Projected **CAGR(Compound Annual Growth Rate)** of **62%** during the Forecast Period

## Global Green Hydrogen Market

### Market Size Overview

**62%**

Global market CAGR,  
2024 - 2029



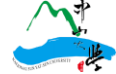
**USD 21.69 Billion** by 2029  
from **USD 1.94 Billion** in  
2024

www.marketdataforecast.com

Source: Market Data Forecast Analysis

The Green Hydrogen Market's expansion is primarily fueled by government initiatives promoting green hydrogen and renewable energy, driven by growing concern over environmental degradation.

Sources: <https://www.globenewswire.com/news>

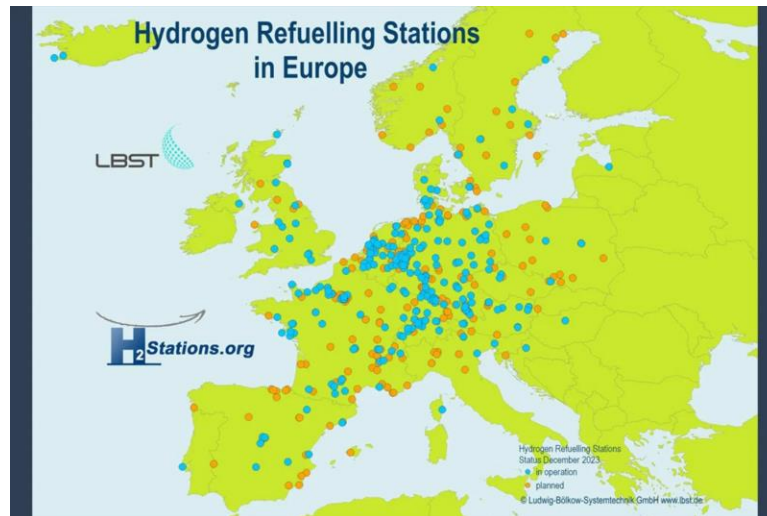


# 2030 in the Net Zero Emission

Low-emission hydrogen is essential for decarbonizing heavy industry, long-distance transport, and steelmaking.

- For highly energy-intensive transport (aviation and shipping).
- In road transport, hydrogen fuel cell electric vehicles (FCEVs) more efficient than EV.
- New applications in industry are critical in steelmaking.

## Hydrogen Refuelling Stations Worldwide



Infrastructure for hydrogen use in transport is expanding-more than over **1160 hydrogen refueling stations** in operation at the mid-2025.

✓ **Czech Republic: 4**

✓ **Euro: 186**

✓ **Japan: 181**

✓ **China: 540**

✓ **Korea: 198**

✓ **Germany: 113**

✓ **United States: 89**

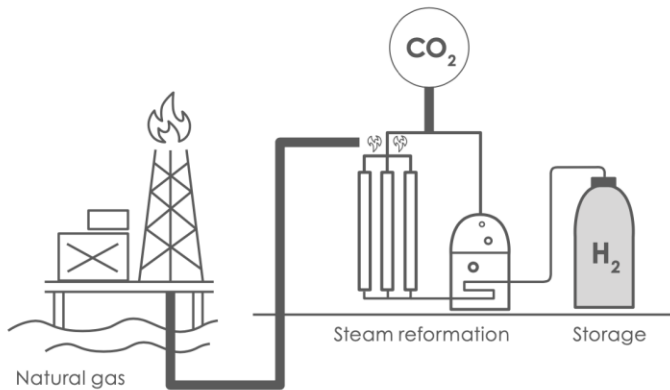
✓ **Taiwan: 1**





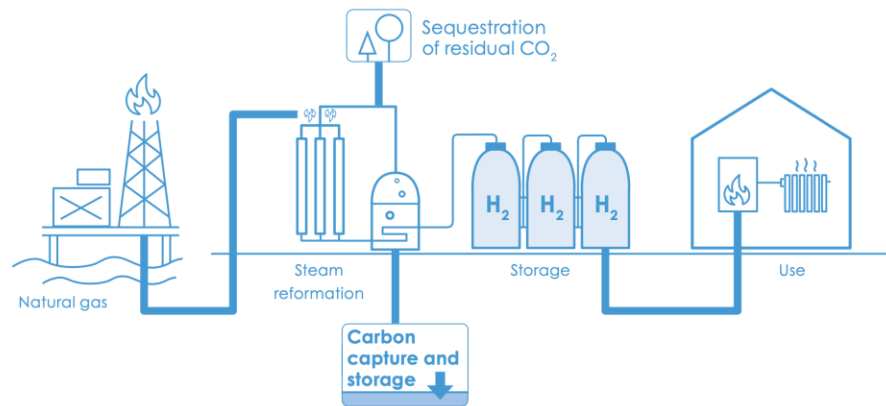
## Grey hydrogen, how hydrogen is currently made

### Grey hydrogen



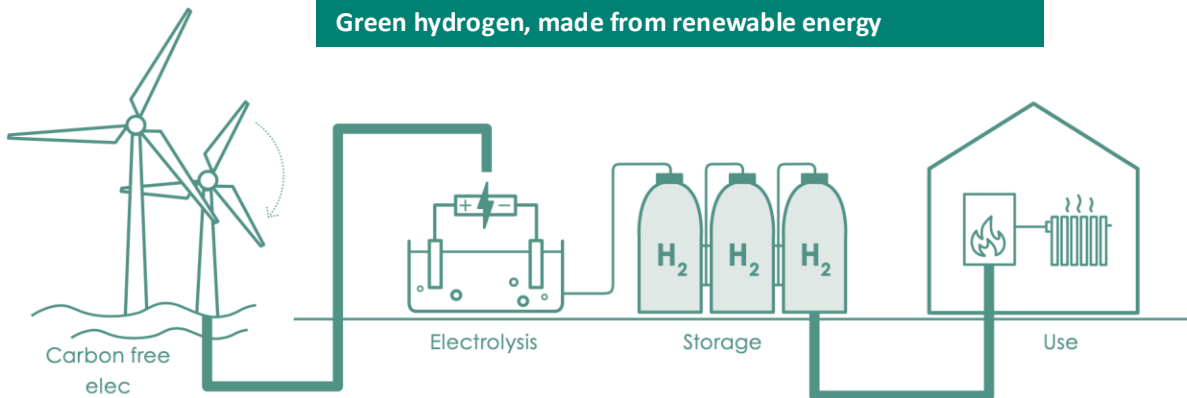
## Blue hydrogen, as advocated by the gas supply industry

### Blue hydrogen



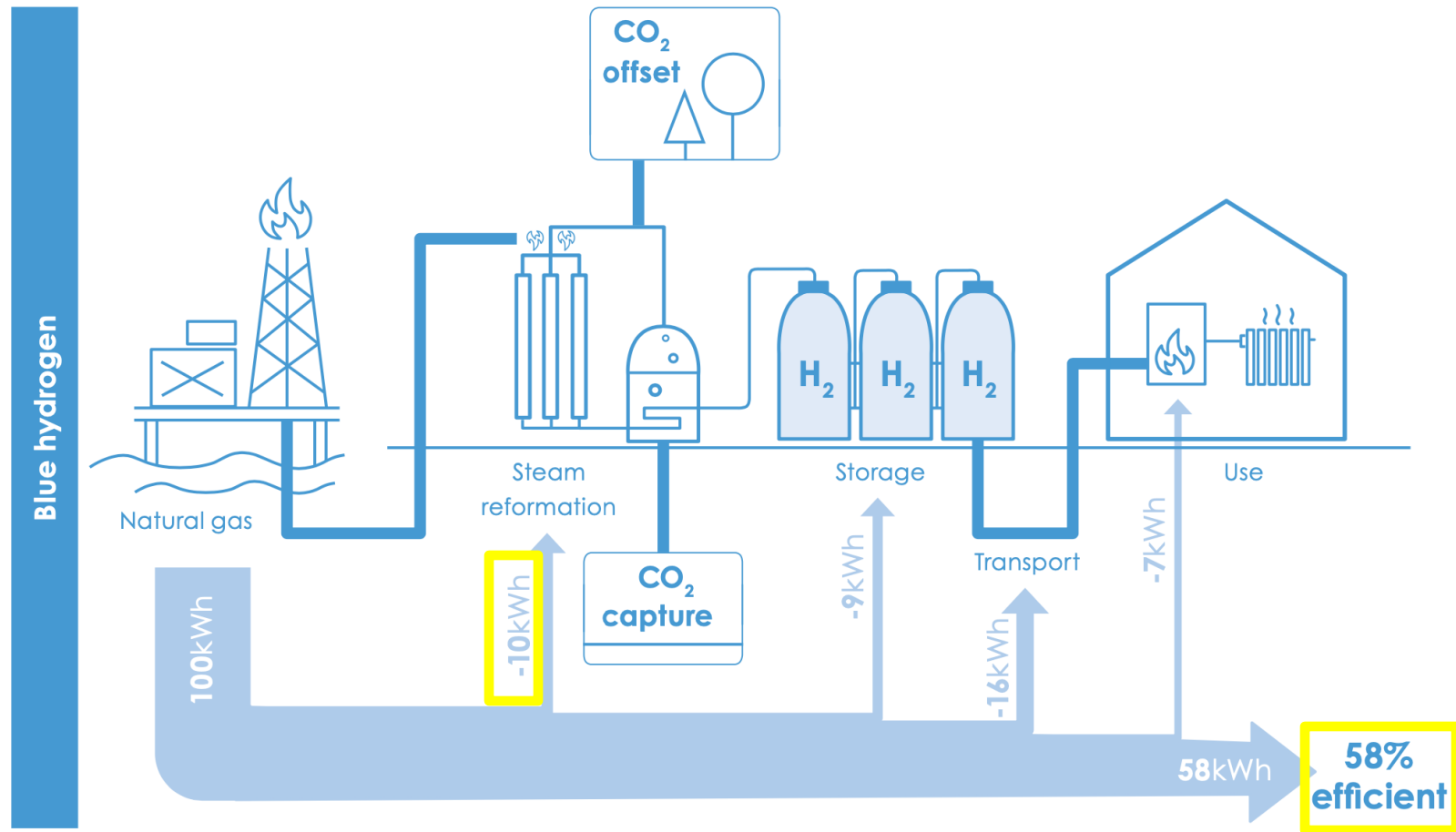
## Green hydrogen, made from renewable energy

### Green hydrogen

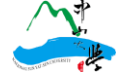




## Blue H<sub>2</sub> Production Emission

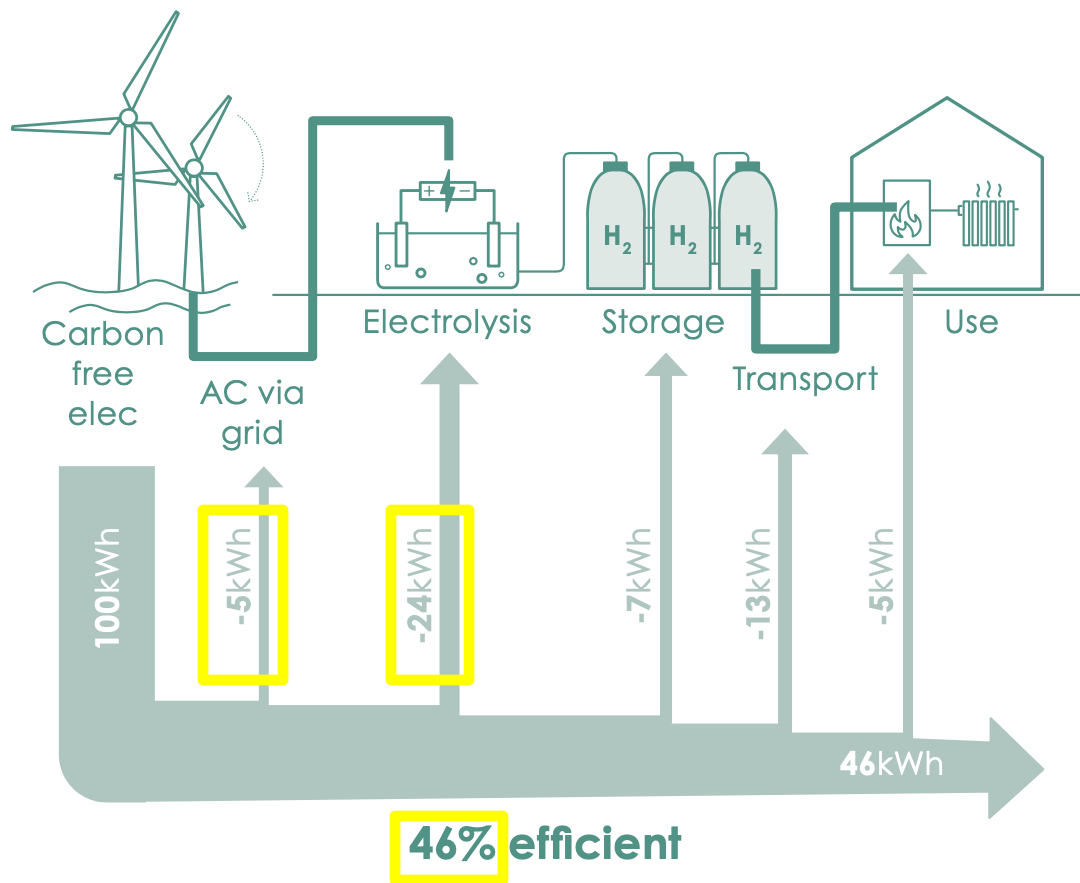






## Green H<sub>2</sub> Production Emission

### Green hydrogen

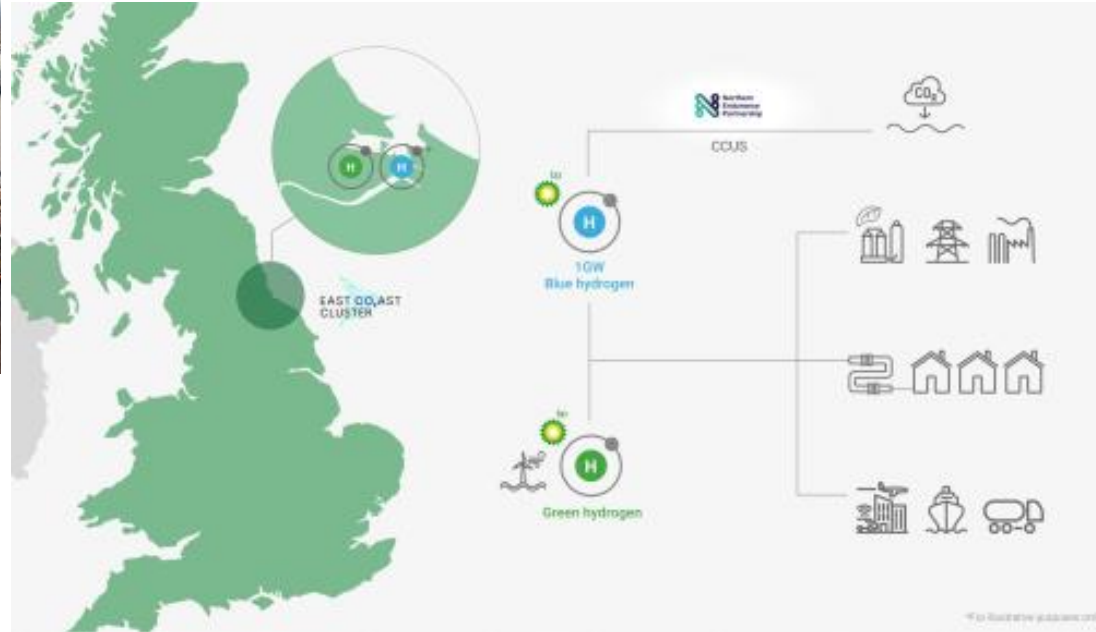
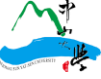


**Hydrogen** as an **energy delivery carrier** is relatively inefficient compared with using renewable electricity with heat pumps

Hydrogen could provide useful renewable energy storage until needed for **winter peaks**.

However, this can be more efficiently implemented using re-purposed combined cycle gas turbine (CCGT) power stations without needing more comprehensive gas grid conversion.

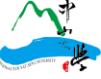
# BP plans UK's largest **blue** and **green** hydrogen **1 GW** project in the Tees Valley in 2017



Sources: <https://www.offshore-energy.biz/rwe-teams-up-with-kellas-midstream-for-green-hydrogen-production/>



# World largest hydrogen fuel cell power plant was built in Korea by KOSPO – 135 MW (2025)

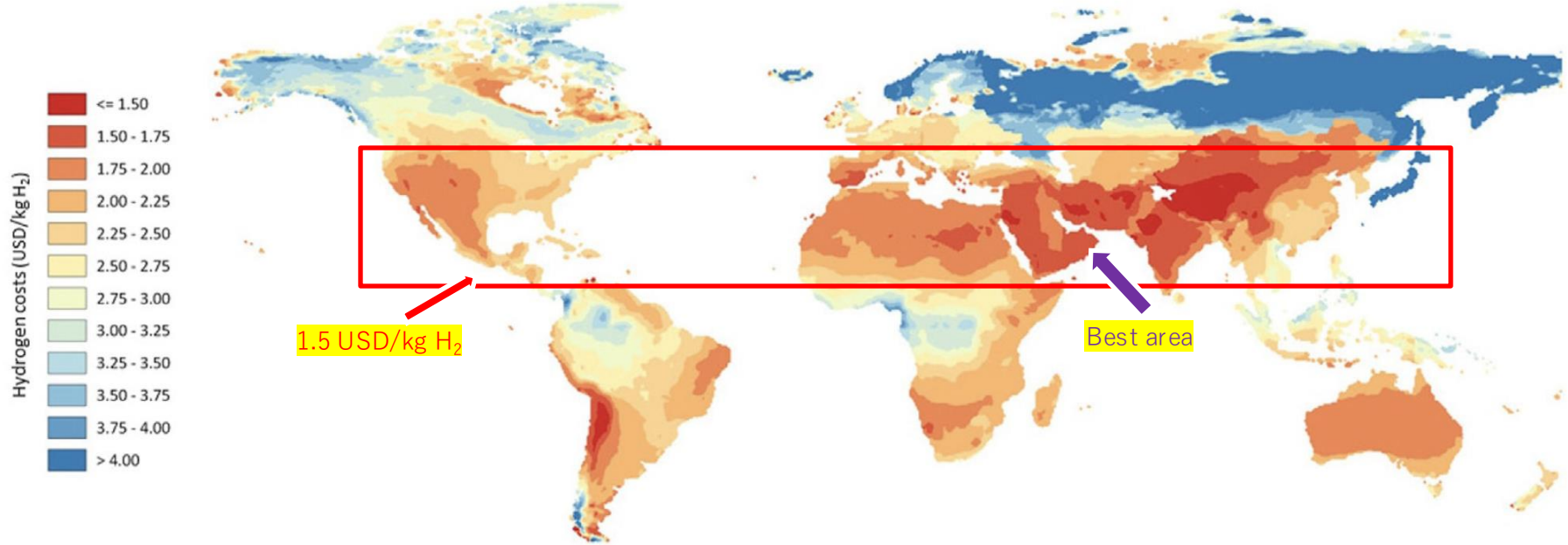
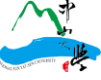


- It is in operation in 2021.
- Capable of providing electricity to some **250,000 households**.
- The project cost about \$300 million.
- It emits little SOX and NOX.
- It can purify fine dust emitted from a nearby liquefied natural gas (LNG) thermal power plant run by **KOSPO**.
- It would also produce hot water for **heating** that can be used by about **44,000 households**.



**SOFC power plant**

# Hydrogen production cost from the hybrid solar cell and wind power in 2030.

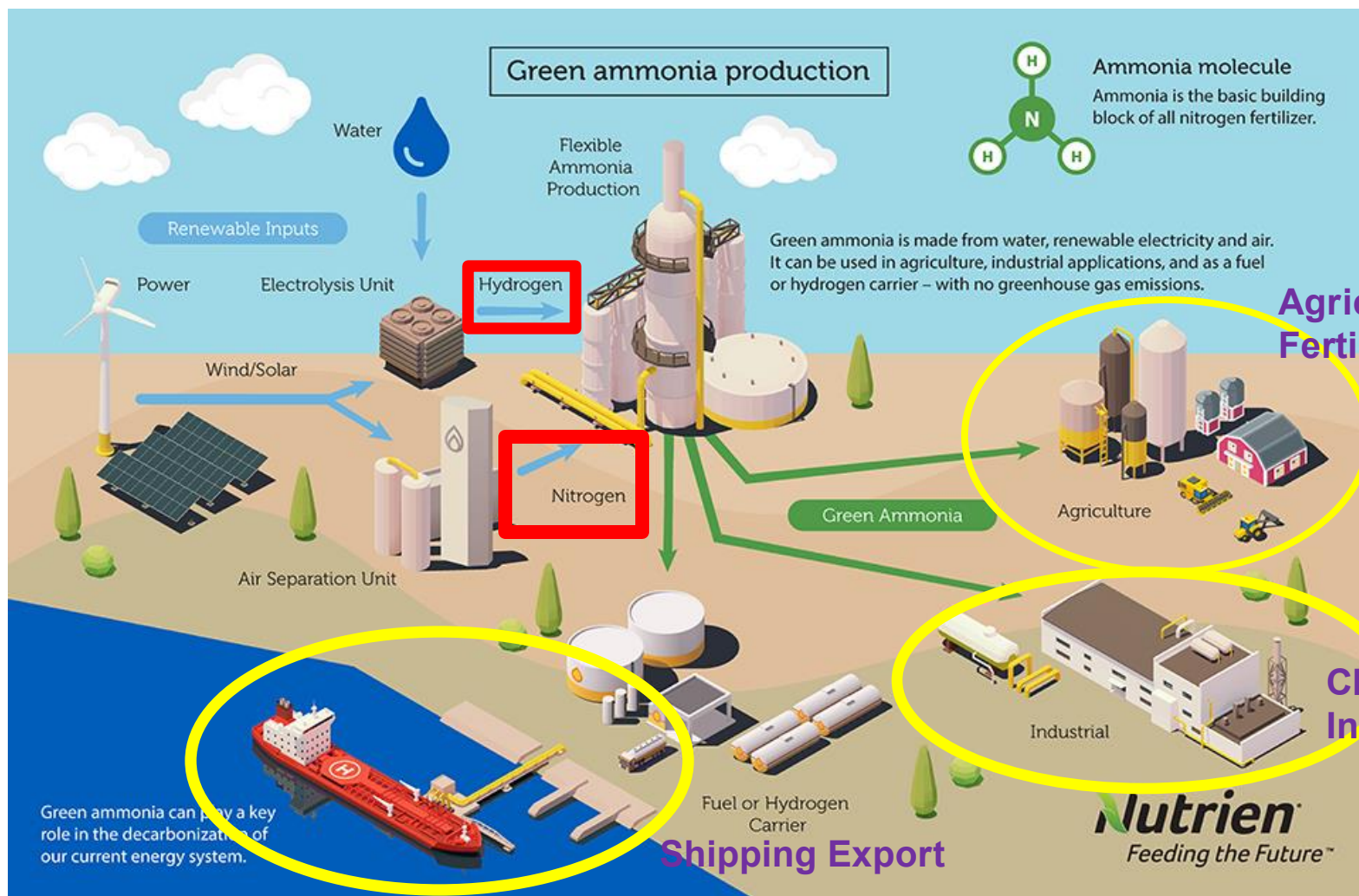


✓ This area is very suitable for solar green energy generation.

✓ 1.5 USD/kg H<sub>2</sub> that would place it as one of the **cheapest green hydrogen producer** in the world.

Source:  
<https://www.researchgate.net/publication/361926388>







# Blue Hydrogen Risks and Dependencies

## ➤ Dependence on CCS technology

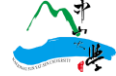
- A **cost-effective** scaling up of CCS technology and capacity is essential.

## ➤ Dependence on fossil fuel supply

- International market fluctuations will directly impact the **cost of production**.

## ➤ Emissions from the production

- Mainly **methane**.



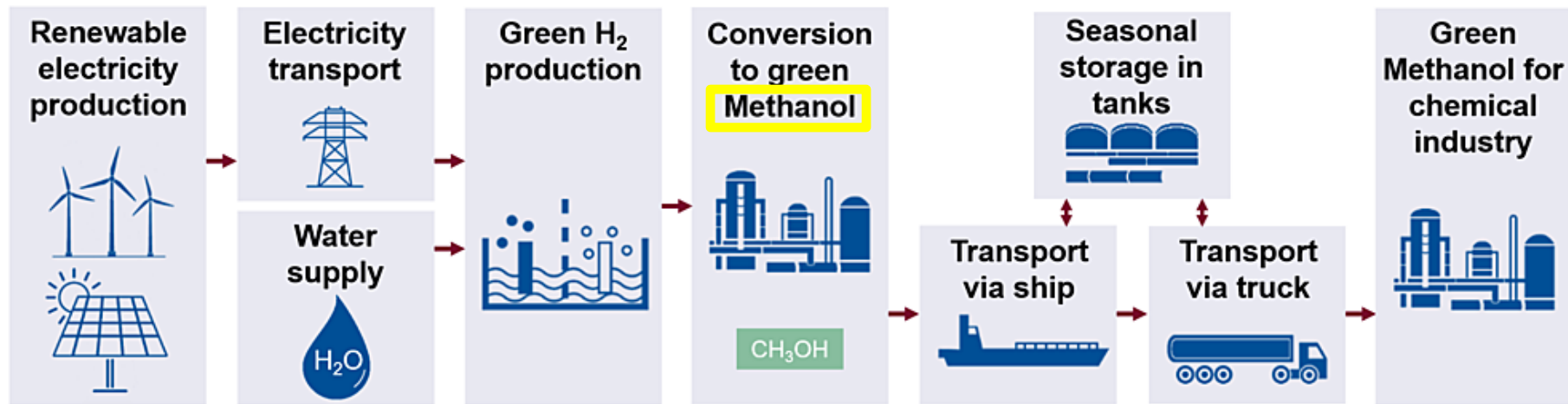
# Blue Hydrogen Risks and Dependencies

- **Dependence on renewable electricity generation and supply**
  - Significant expansion of renewable energy capacity.
- **Competition for renewable energy between direct electrification and green hydrogen production**
- **Electrolyser build rates and supply of the critical raw materials required**
  - Rising global demand could cause price fluctuations and potentially lead to geopolitical issues.
- **Access to sufficient water supply and sufficient waste management systems, together with the availability and access to renewable electricity**
  - Are crucial factors in determining green production's location and environmental impact.





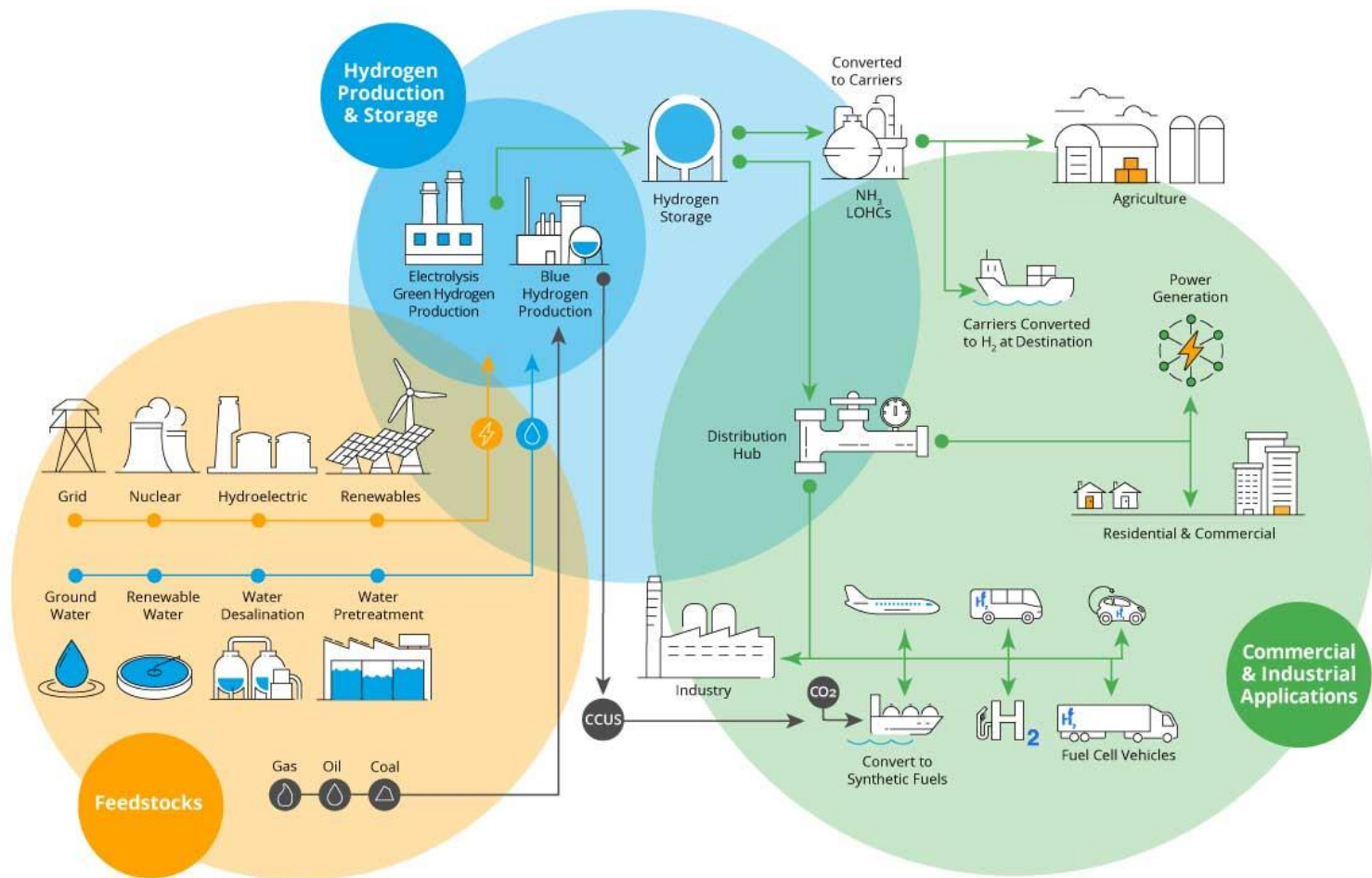
The various components can be combined in the hydrogen transmission and distribution value chain, leading to specific **cost benefits**.

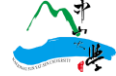


**Green methanol production for chemical industry**



# Safe, Reliable, and Informed Innovation Across the Hydrogen Value Chain

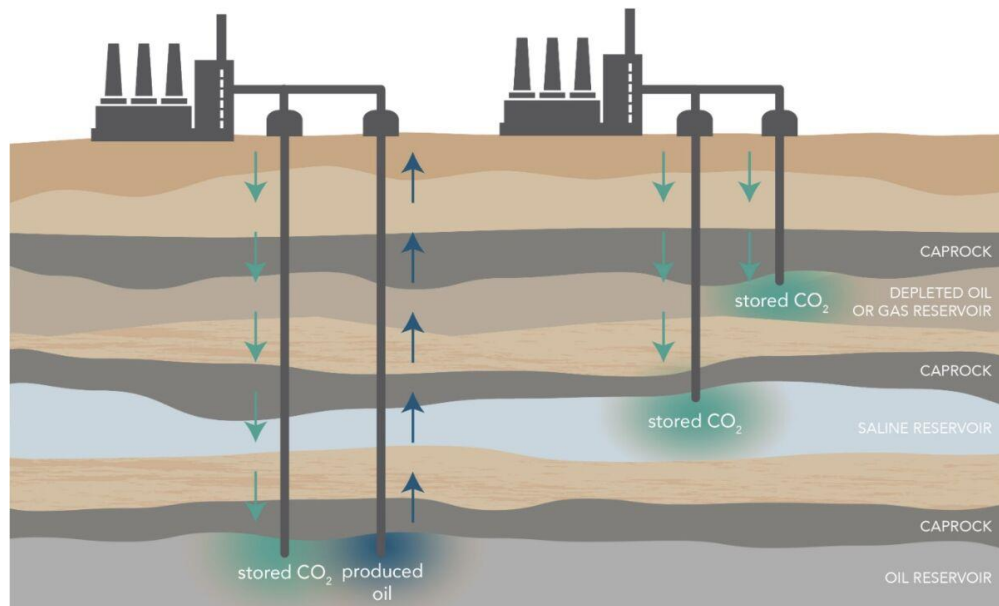




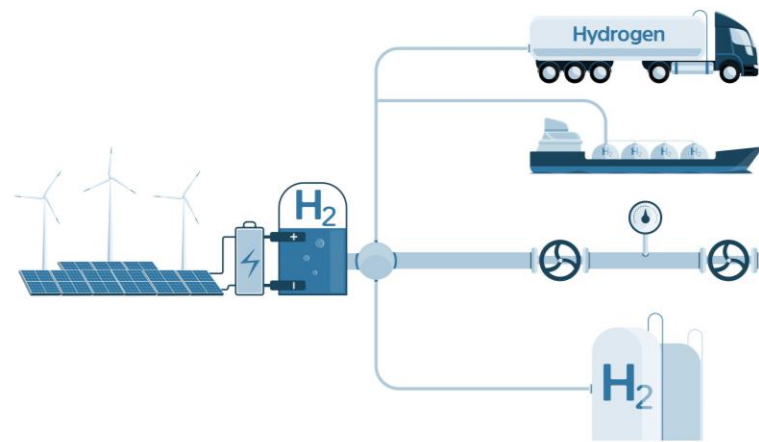
# Hydrogen storage

Today hydrogen is most commonly stored as a gas or liquid in tanks for small-scale mobile and stationary applications.

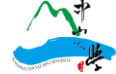
- **Geological storage**
  - The best option for **large-scale** and long-term storage.



- **Storage tanks**
  - The more suitable for **short-term** and small-scale storage.



# Hydrogen Transmission and Distribution

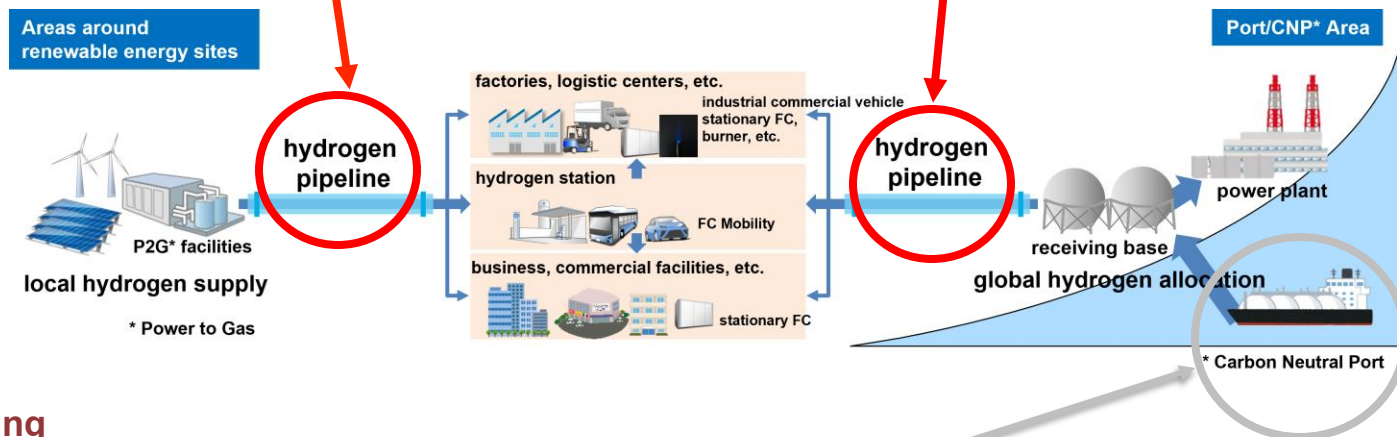


- The low energy density of hydrogen means that it can be **very expensive** to transport over long distances.
- Natural gas, pure hydrogen, can be liquefied **before** being transported to increase density.
- Incorporate the hydrogen into large molecules that can be more readily **transported as liquids**.
- IEA analysis indicates that hydrogen transmission as a gas by pipeline is generally the **cheapest option** if the hydrogen needs are transported for more than 1500 km.

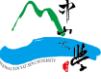


# Hydrogen Transmission and Distribution

- Transporting energy over long distances is **easier** when the energy is a chemical fuel rather than electricity.
- Pipelines**
  - It can be used for a long time (40-80 years).
  - Their two main **drawbacks** are
    - a. the high capital costs entailed.
    - b. the need to acquire the right of way by necessity (Country to Country).



- Shipping**
  - Imported hydrogen offers scope for countries to diversify their energy imports, and one result of this is **significant interest** in using **ships to transport hydrogen**.



# Potential Roles of Hydrogen in Future Energy Systems

- ✓ **Industry**
- ✓ **Transport**
- ✓ **Heat and Building**



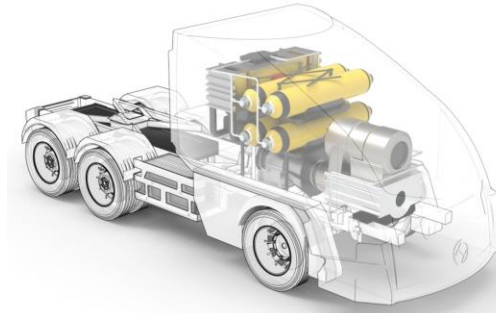
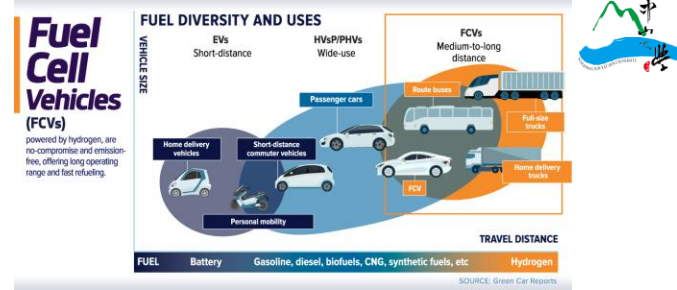
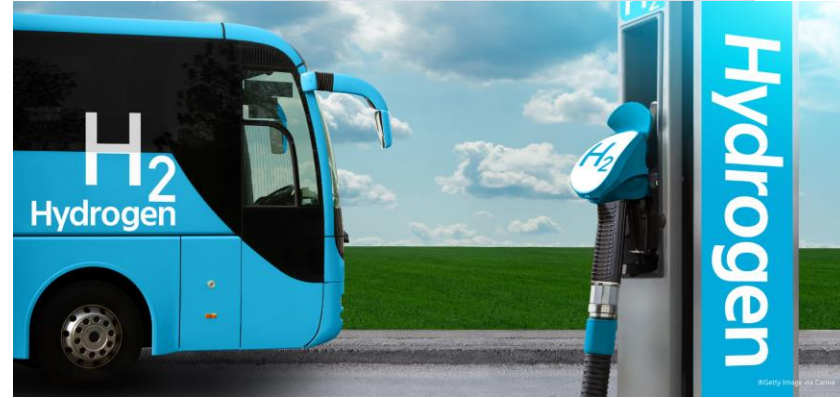
# Industry

- **Chemical industrial processes**
  - The **hydrogen** demand for **methanol production** will likely **increase** from plastic production shifts away from fossil fuel-based production processes.
- **Primary steelmaking**
  - Hydrogen can substitute fuels as the **sole reducing agent** to produce direct reduced iron and water instead of  $\text{CO}_2$  as a by-product.
- **Industrial heating**
  - Hydrogen is likely to be the **only** option available to substitute fossil fuel in certain industrial direct-firing processes (such as furnaces and kilns).



# Transport

- Heavy goods vehicles and public service vehicles  
- Hydrogen fuel cell electric vehicles.

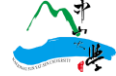


Source: <https://www.innovationnewsnetwork.com/bmw-brings-a-revolutionary-fleet-of-hydrogen-vehicles-to-our-roads/30656/>

# Transport

- **Shipping**
  - Hydrogen-derived fuels such as ammonia will likely be the most widely adopted option.

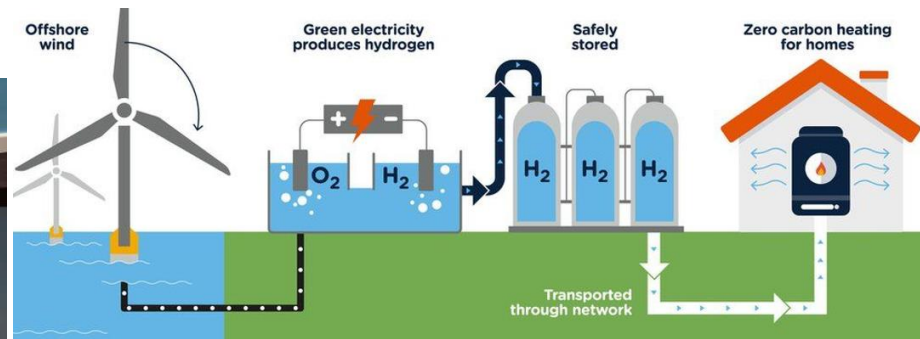




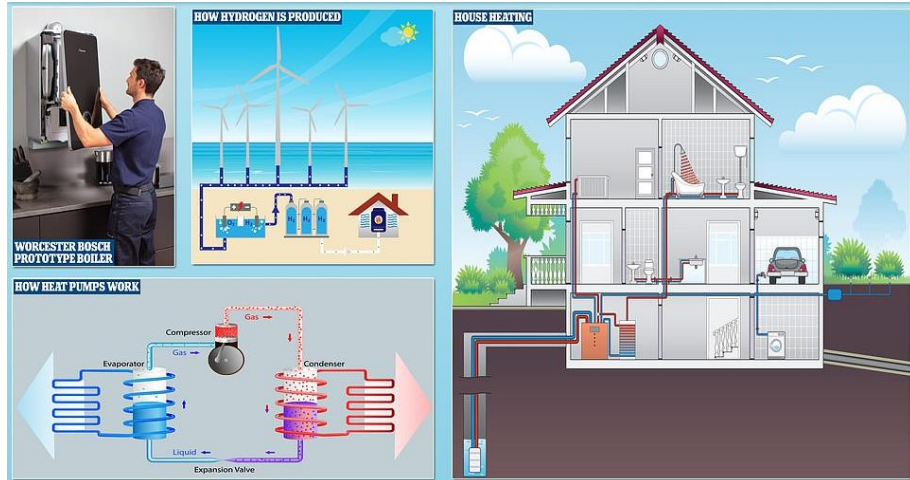
# Heat and Building

- Domestic heating

- As the UK strives to meet its ambitious climate targets, decarbonizing the way we heat our homes and workplaces has become a key focus. Currently, heating accounts for nearly a quarter of the UK's carbon emissions, with around **85%** of homes relying on **natural gas**. While technologies like heat pumps and heat networks are gaining traction, **hydrogen heating** is emerging as a potential alternative.

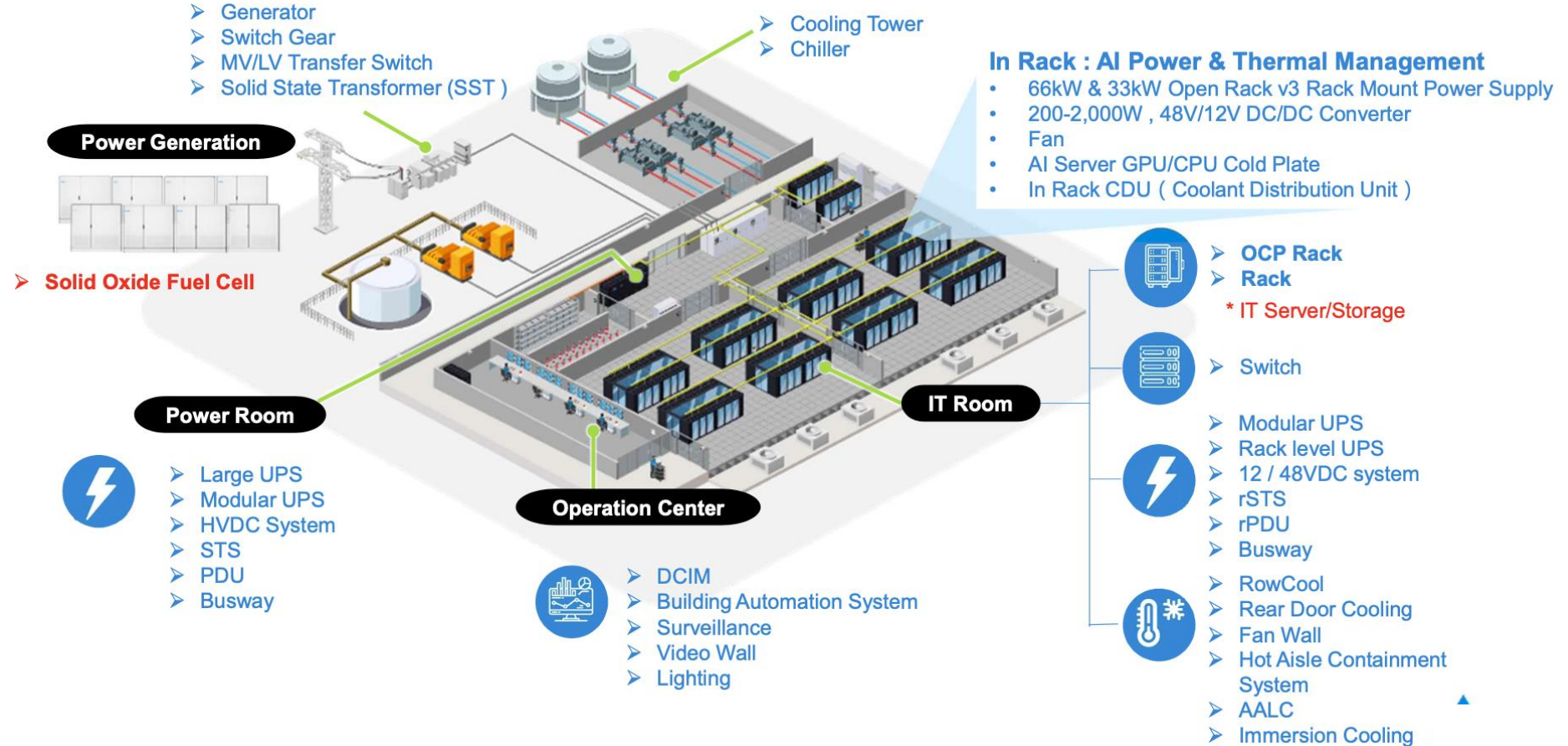
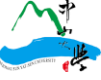


Hydrogen heating could be coming to the UK in 2026 based on the government's heating strategy (Image credit: BDR Therma)l

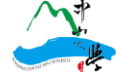




# AI Datacenter Power Solution



# Benefits to Implement SOFC into Data Center as Primary Power



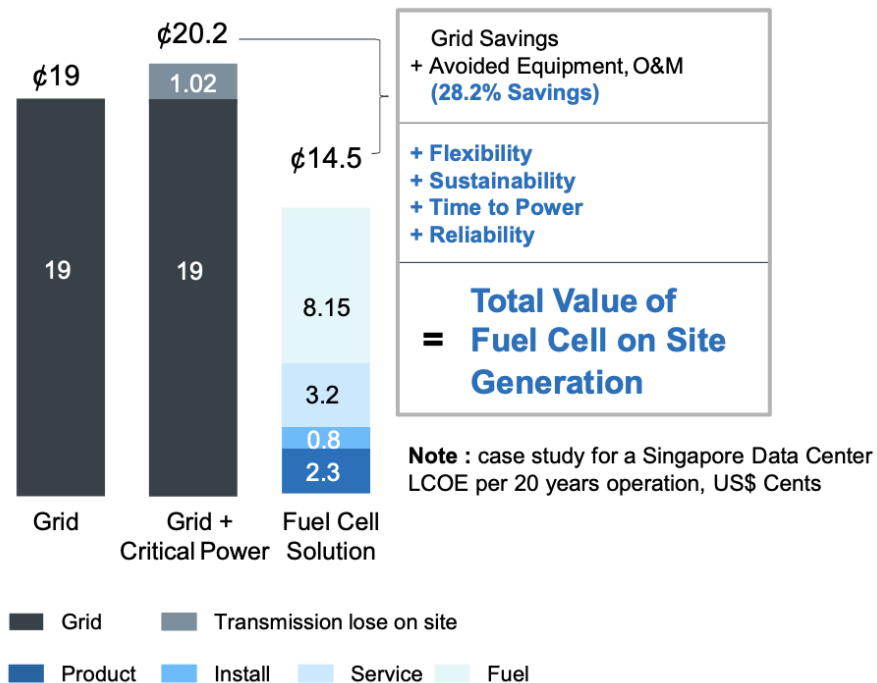
1. Lower  $CO_2$  emission about -27% if no CCUS
2. Wider power sources options , easier for some countries those hard to have MW power supply
  - A. Natural Gas
  - B. Bio Gas
  - C. Hydrogen
  - D. Ammonia
3. Higher availability by having more energy sources to minimize the potential risk of single power sources failure .
4. High temperature fuel cell as SOFC to integrate with absorption cooling system for another energy saving
5. Possible to offer the DC power output direct to DC powered IT as stack originally generated DC power , higher efficiency

# Attractiveness of Critical Load Users Fuel Cell Distributed Prime Power Generation

Sustainability	Flexibility
<ul style="list-style-type: none"> <li>40g CO<sub>2</sub> / kWh emission saving than Grid</li> <li>Energy saving with heat recycle and absorption cooling</li> </ul>	<ul style="list-style-type: none"> <li>Multiple fuel options, Natural gas, Biogas, H<sub>2</sub></li> <li>AC or DC power output</li> <li>Option to recycle the heat with absorption cooling</li> <li>110kW per module, modular design for expansion</li> </ul>
Time to Power	Reliability
<ul style="list-style-type: none"> <li>24 months to 9 months</li> <li>Optimized the cash flow of REIT/colocation builder</li> </ul>	<ul style="list-style-type: none"> <li>Distributed power generation to minimize the power outage of centralized grid</li> <li>Robust gas pipelines to minimize the disaster impact</li> <li>Easier buffer gas tank for long time backup</li> </ul>

REIT : Real Estate Investment Trust

## 20Yrs Levelized Cost of Electricity (¢/kWh)



# Benefits with SOFC as Primary Power in Data Center

- Power Generation Sources Changed

Scenario	Existing Power Architecture	SOFC Architecture
Primary Power	Utility	SOFC with Natural Gas
Short Term backup	UPS + Li-Ion Battery	UPS + Li-Ion Battery
Backup power	Diesel Generator	Utility

- Advantages



**1** Minimize the potential outage of centralized power generation



**2** Time to get power permission



**3** Same site to expand for higher power density



**4** Eliminate the diesel generator



**5** Lower CO2 emission

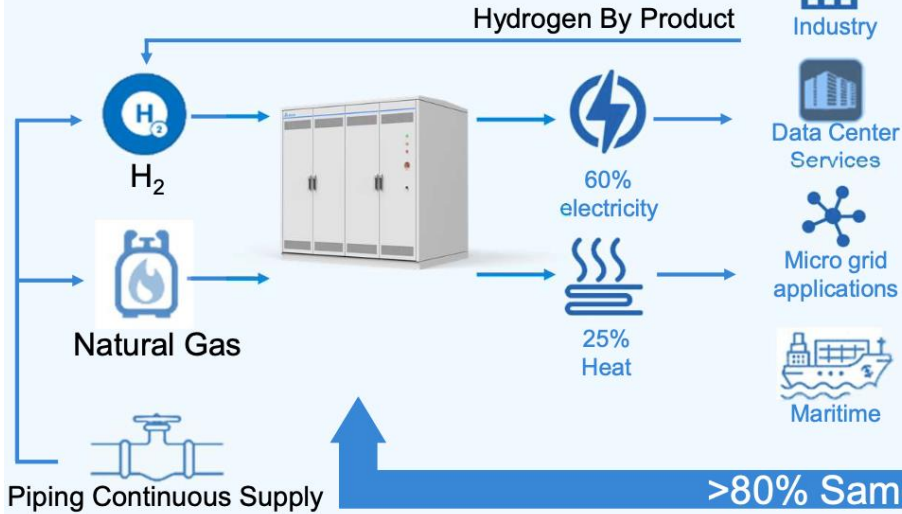


**6** Heat recycle with Absorption Chiller

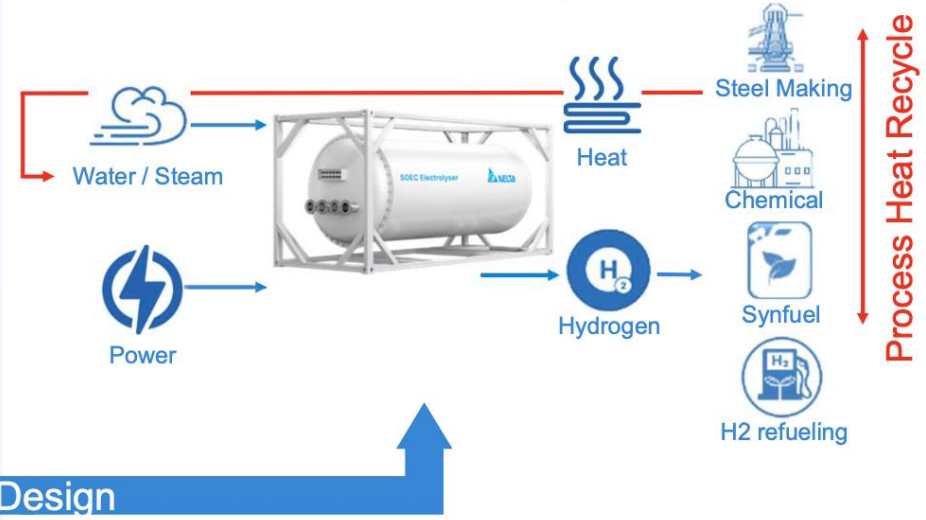


# Delta's Target Technology & Application

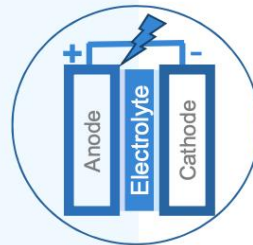
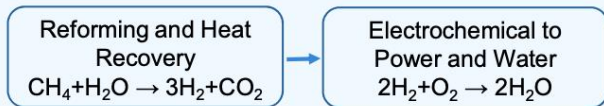
## Solid Oxide Fuel Cell



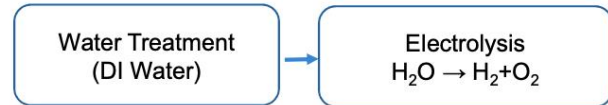
## Solid Oxide Electrolysis Cell

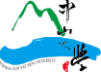


## Power Generation



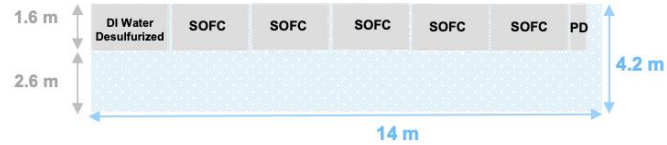
## Hydrogen Production



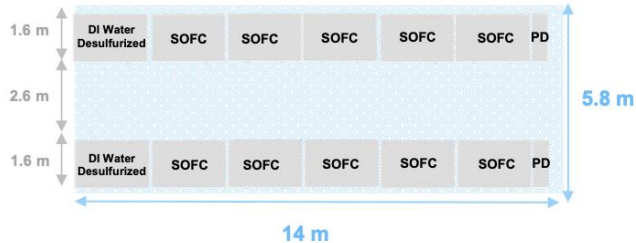


# Modular Design - Capacity Expanded

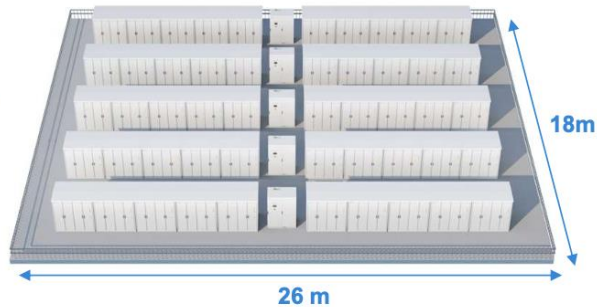
**C&I 550kW System**



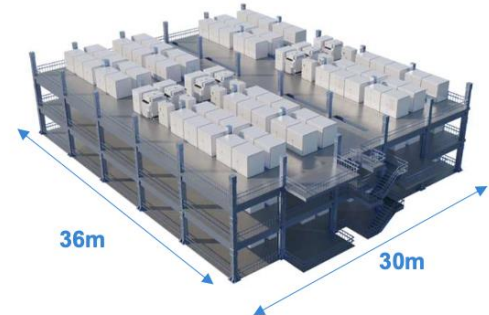
**1.1MW Centralized System**



**5.5MW Centralized System**



**25MW Power Tower Concept**

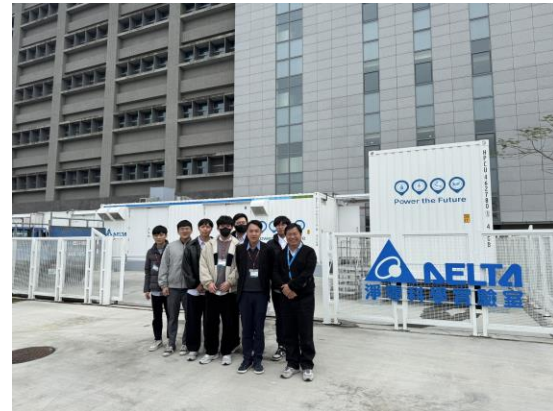




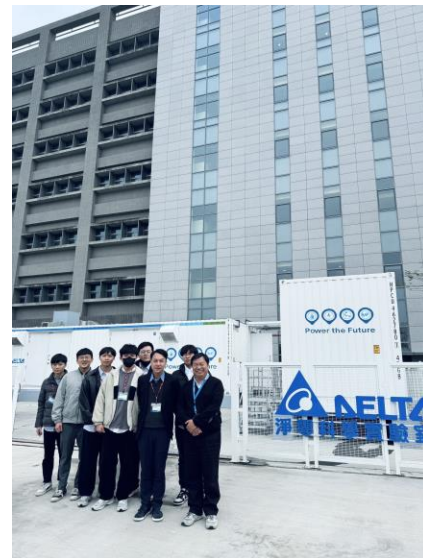
# Key Messages

Fuel Options	<ul style="list-style-type: none"><li>• Natural Gas</li><li>• Hydrogen (H<sub>2</sub>) – Future model</li><li>• Ammonia (NH<sub>3</sub>) – Future model</li></ul>
Efficiency (LHV)	<ul style="list-style-type: none"><li>• 53% ~ 63% (Electricity Generation )</li></ul>
Life	<ul style="list-style-type: none"><li>• Stack : &gt;40KHrs (EOL: LHV &gt; 53%) · Capable for operation after 40KHrs</li><li>• System : &gt;15 Years</li></ul>
Continues Operation	<ul style="list-style-type: none"><li>• 24/7 non-stop and continues power generation</li><li>• Capacity factor &gt; 95%</li></ul>
Fuel Consumption	<ul style="list-style-type: none"><li>• Natural Gas 1M<sup>3</sup> = about 5.5kWh</li></ul>
CO <sub>2</sub> Emission Intensity	<ul style="list-style-type: none"><li>• &lt;360g/kWh ( fuel as natural gas )</li></ul>
After Service	<ul style="list-style-type: none"><li>• 1<sup>st</sup> year as free warranty upon handover</li><li>• Service level agreement from 2<sup>nd</sup> years onwards</li></ul>

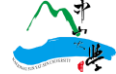
# Delta Net Zero Science Lab



Delta, a global leader in power management and a provider of IoT-based smart green solutions, inaugurated today Taiwan's 1st megawatt (MW)-grade R&D lab for water electrolysis hydrogen production and for fuel cells, the "Delta Net Zero Science Lab," at its Tainan Plant 2. This significant milestone provides a diverse testing environment for component and system validation of hydrogen production and fuel cell technologies.



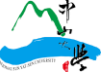
# Comparison of Solid Oxide Fuel Cell Types



- SOFC have advantages such as **high energy efficiency**, **fuel flexibility**, and **low environmental impact**.

	TSOFC (Tubular SOFC)	CS-SOFC and AS-SOFC (Cathode-Supported SOFC, Anode-Supported SOFC)	ES-SOFC (Electrolyte-Supported SOFC )	MS-SOFC (Metal-Supported SOFC)
Advantage	<ul style="list-style-type: none"> <li>• Good sealing</li> <li>• More robust and stable structure</li> <li>• Stronger thermal cycling capability</li> </ul>	<ul style="list-style-type: none"> <li>• Lowering the internal resistance</li> <li>• Lower temperatures</li> </ul>	<ul style="list-style-type: none"> <li>• Simplify the battery structure.</li> <li>• Better long-term stability</li> </ul>	<ul style="list-style-type: none"> <li>• Enhance structural strength</li> <li>• Resistance to thermal stress.</li> <li>• Electrode thickness</li> <li>• Better thermal conductivity</li> </ul>
Defect	<ul style="list-style-type: none"> <li>• Complex manufacturing processes</li> <li>• Higher costs</li> <li>• Higher internal resistance</li> <li>• Lower efficiency.</li> </ul>	<ul style="list-style-type: none"> <li>• Longer startup time</li> <li>• Special structure and materials</li> <li>• The current density of CS-SOFC is lower than that of AS-SOFC.</li> </ul>	<ul style="list-style-type: none"> <li>• higher internal resistance</li> <li>• lower efficiency</li> <li>• relatively low structural strength</li> </ul>	<ul style="list-style-type: none"> <li>• Fuel corrosion</li> <li>• Special materials treatment and design</li> </ul>





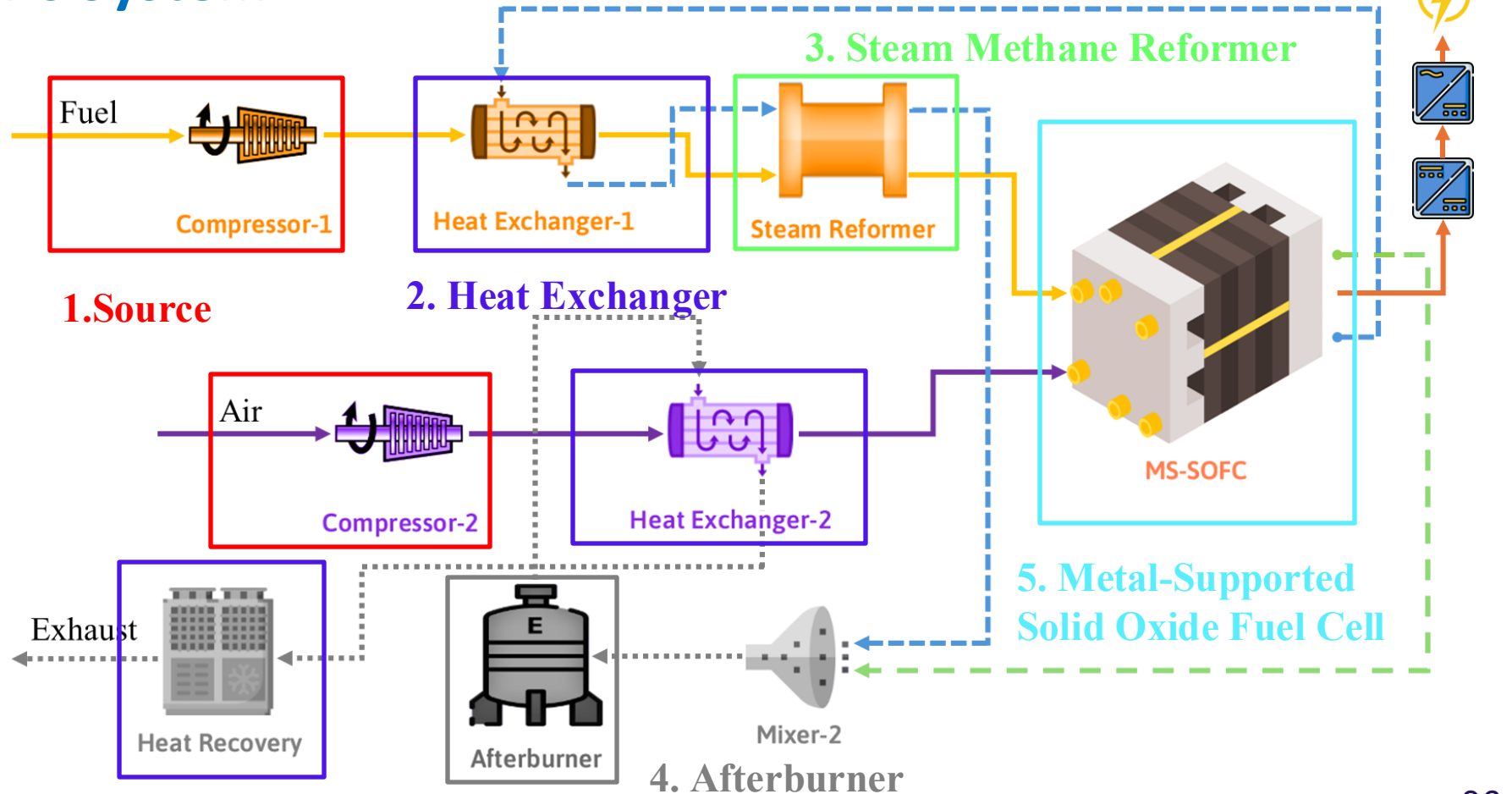
Emerging **MS-SOFC** designs offer several important advantages over traditional designs, including lower-to-medium operating temperatures, enhanced thermal response capabilities, and shorter startup times.

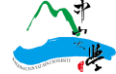
They are thus considered to have significant commercial potential. However, their performance under different fuel conditions is not yet clear.

1. Accordingly, in recent research, stack model simulations were performed to investigate the current density, voltage, temperature distribution, and fuel cell fractions in a typical **MS-SOFC** design operated with either pure hydrogen fuel or mixed fuel with various **water-to-carbon ratios (S/C)** and methane vapor reforming reaction rates.
2. The purpose of the simulations was to establish the operating parameters that optimized the current density and overall performance of the MS-SOFC under low-temperature conditions of 600 °C.



# SOFC System





## Mass balances

1. Fuel Channel
2. Air Channel
3. Chemical Reaction

## Energy balances

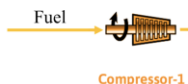
1. Fuel Channel
2. Air Channel
3. PEN structure
4. Interconnect

## Electrochemical

1. Nernst equation
2. Ohmic Overpotential
3. Concentration Polarization
4. Activation loss

## Other components

### Source



Ideal gas law

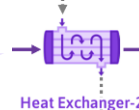
**Peng-Robinson** Equation of  
State (PR-EOS)

### Reformer Afterburner



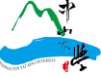
Equilibrium reactor  
Energy balance  
Mass balance

### Heater Heat Exchanger



Energy balance  
Mass balance

# Mass balances



## 1. Fuel Channel

### Concentration of Fuel Channel

$$\frac{\partial C_{i,f}}{\partial t} = -u_f \frac{\partial C_{i,f}}{\partial x} + \sum_{k \in \{(i),(ii),(V)\}} v_{i,k} R_{i,k} \frac{1}{h_f}$$

$$i \in \{CH_4, H_2O, CO, H_2, CO_2\}$$

$C_{i,f}$ : molar concentration of component

### Concentration

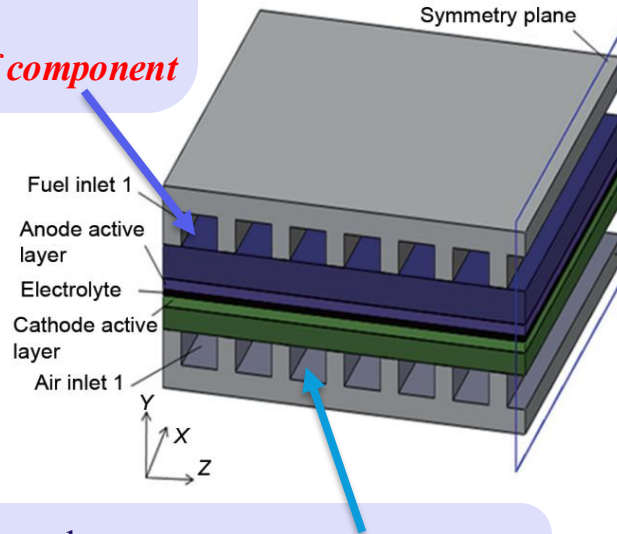
$$PV = nRT, C = \frac{n}{V}$$

$$\Rightarrow C = \frac{n}{V} = \frac{P_i}{R * T_{an}} = \frac{P_{an} * f_i}{R * T_{an}}$$

## 2. Air Channel

$$\frac{\partial C_{i,a}}{\partial t} = -u_a \frac{\partial C_{i,a}}{\partial x} + v_{i,(V)} R_{i,(V)} \frac{1}{h_a}, i \in \{O_2, N_2\}$$

Concentration of Air Channel



## 3. Chemical Reaction

### (i). Electrochemical

$$R_{(i)} = \frac{j}{2F}$$

### (ii). Steam Reforming

$$R_{(ii)} = k_0 p_{CH_4} \exp\left(-\frac{E_a}{RT}\right)$$

### (iii). Gas-shift

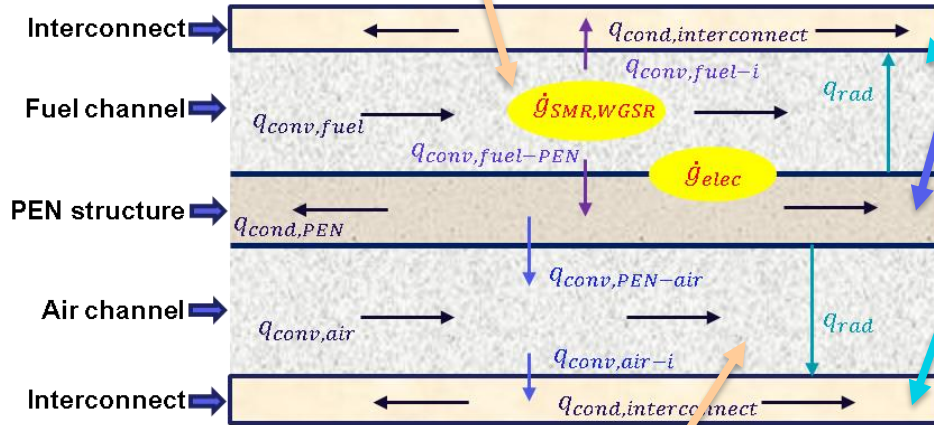
$$R_{(iii)} = k_{WGSR} p_{CO} \left(1 - \frac{p_{CO_2} p_{H_2}}{p_{CO} p_{H_2O}}\right)$$

# Energy balances

## 1. Fuel Channel

$$\rho_f c_{p,f} \frac{\partial T_f}{\partial t} = -u_f \rho_f c_{p,f} \frac{\partial T_f}{\partial x} + k_{f,PEN}(T_{PEN} - T_f) \frac{1}{h_f} + k_{f,I}(T_{PEN} - T_f) \frac{1}{h_f} + \Sigma (-\Delta H)_k R_k \frac{1}{h_f}$$

**Temperature of Anode**



## 2. Air Channel

$$\rho_a c_{p,a} \frac{\partial T_a}{\partial t} = -u_a \rho_a c_{p,a} \frac{\partial T_a}{\partial x} + k_{a,PEN}(T_{PEN} - T_a) \frac{1}{h_a} + K_{a,I}(T_I - T_a) \frac{1}{h_a}$$

**Temperature of Cathode**

## Two-Phase (Solid-Gas)

### 3. PEN structure

*PEN : Positive-electrode/Electrolyte/Negative-electrode*

$$\rho_{PEN} c_{p,PEN} \frac{\partial T_{PEN}}{\partial t} = \lambda_{PEN} \frac{\partial^2 T_{PEN}}{\partial x^2} - k_{f,PEN}(T_{PEN} - T_f) \frac{1}{\tau_{PEN}}$$

**Temperature of PEN structure**

$$-k_{a,PEN}(T_{PEN} - T_a) \frac{1}{\tau_{PEN}} + [(-\Delta H)_{(v)} R_{(v)} - jU] \frac{1}{\tau_{PEN}} + \left[ \frac{\sigma(T_I^4 - T_{PEN}^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_{PEN}} - 1} \right] \frac{1}{\tau_{PEN}}$$

### 4. Interconnect

**Temperature of Interconnect**

$$\rho_I c_{p,I} \frac{\partial T_I}{\partial t} = \lambda_I \frac{\partial^2 T_I}{\partial x^2} - k_{f,I}(T_I - T_f) \frac{1}{\tau_I} - k_{a,I}(T_I - T_a) \frac{1}{\tau_I} - \left[ \frac{\sigma(T_I^4 - T_{PEN}^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_{PEN}} - 1} \right] \frac{1}{\tau_I}$$

### Specific heat capacity

$$c_{p,ca} = 0.92f_{O_2} + 1.04f_{N_2}$$

$$c_{p,an} = 14.3f_{H_2} + 2.156f_{H_2O} + 2.156f_{CH_4} + 2.21f_{CO} + 0.8f_{CO_2}$$

### Density of the gas steams

$$PV = nRT = \frac{m}{M} RT \longrightarrow \rho_{an} = \frac{m}{V} = \frac{PM}{RT} = \sum \frac{P_i M_i}{RT_{an}}$$

$$U = U_{TPB}^{OCP} - (\eta_{Ohm} + \eta_{conc,anode} + \eta_{conc,cathode} + \eta_{act,anode} + \eta_{act,cathode})$$

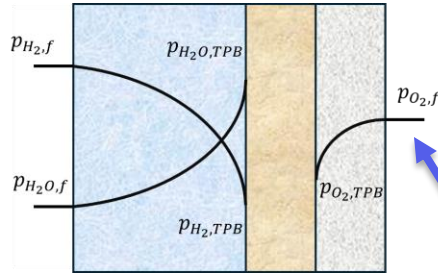
## Nernst equation

TPB : Three-Phase Boundaries

$$U_{TPB}^{OCP} = U_{H_2}^0 - \frac{RT}{2F} \ln \left( \frac{p_{H_2O,TPB}}{p_{H_2,TPB} p_{O_2,TPB}^{0.5}} \right)$$

$$p_{H_2,TPB} = p_{H_2,f} - \frac{RT\tau_{anode}}{2FD_{eff,anode}} j$$

Gas distribution diagram at the three-phase boundary in SOFC



$$p_{O_2,TPB} = P - (P - p_{O_2,a}) - \frac{RT\tau_{anode}}{4FD_{eff,cathode}} j$$

$$p_{H_2O,TPB} = p_{H_2O,f} - \frac{RT\tau_{anode}}{2FD_{eff,anode}} j$$

## Polarization

### Ohmic Overpotentials

$$\eta_{Ohm} = jR_{Ohm}, R_{Ohm} = \frac{\tau_{anode}}{\sigma_{anode}} + \frac{\tau_{electrolyte}}{\sigma_{electrolyte}} + \frac{\tau_{cathode}}{\sigma_{cathode}}$$

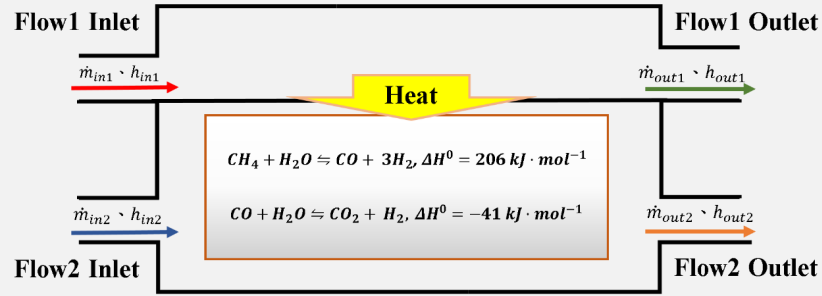
### Concentration Polarization

$$\eta_{conc} = \frac{RT}{2F} \ln \left( \frac{p_{H_2O,TPB} p_{H_2,f}}{p_{H_2,TPB} p_{H_2O,f}} \right) + \frac{RT}{4F} \ln \left( \frac{p_{O_2,a}}{p_{O_2,TPB}} \right)$$

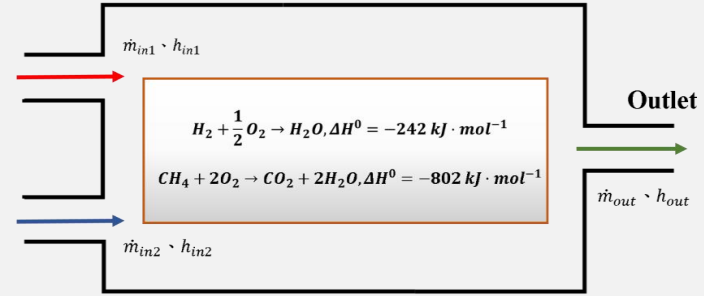
### Activation loss

$$j = j_{0,electrode} \left[ \exp \left( \frac{\alpha n F}{RT} \eta_{act,elect} \right) - \exp \left( - \frac{(1-\alpha) n F}{RT} \eta_{act,elect} \right) \right] \exp \left( \frac{E_{electrode}}{RT} \right)$$

## Steam Methane Reformer and Afterburner



Flow 1 (Anode Outlet)



Flow 2 (Cathode Outlet)

**Equilibrium reactor:** General chemical reaction formula:  $aA + bB \rightleftharpoons cC + dD$

**Equilibrium constant**  $\ln(k) = \frac{\Delta G}{RT}$   $\Rightarrow k = \left( \frac{\psi_C^c \cdot \psi_D^d}{\psi_A^a \cdot \psi_B^b} \right) \cdot \left( \frac{p}{p_0} \right)^{\Delta n}$   $\Rightarrow \Psi$ : mole fractions of each species at equilibrium in a chemical reaction

**Mass balance**  $\frac{dm}{dt} = \sum \dot{m}_{out} - \sum \dot{m}_{in}$  **Energy balance**  $\frac{dU}{dt} = \sum \dot{H}_{in,i} + \sum \dot{H}_{out,i} + \sum \dot{Q}_k$

$\Delta G$  = Gibbs free energy changes



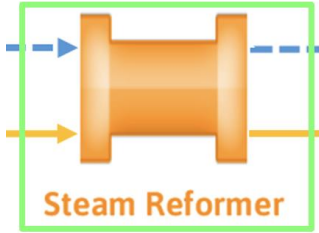
# Other components

Source

$$Z \times R \times T = p \times v$$

➡  $Z=1$ , ideal gas

➡  $Z \neq 1$ , Peng-Robinson Equation of State, PR-EOS



$$P = \frac{RT}{V_m - b} - \frac{a\alpha}{V_m^2 + 2bV_m - b^2}$$

$$a = \frac{0.4572R^2T_c^2}{P_c}$$

$$b = \frac{0.0778RT_c}{P_c}$$

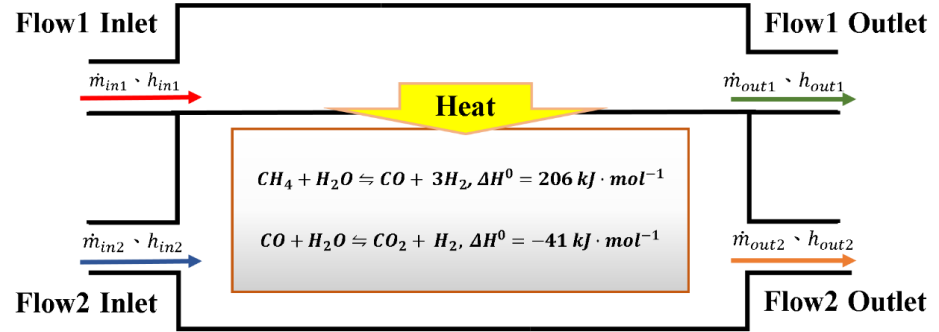
$$Z^3 - (1 - B)Z^2 + (A - 2B - 3B^2)Z - (AB - B^2 - B^3) = 0$$

$$A = \frac{a\alpha P}{R^2T^2}, B = \frac{bP}{RT}$$

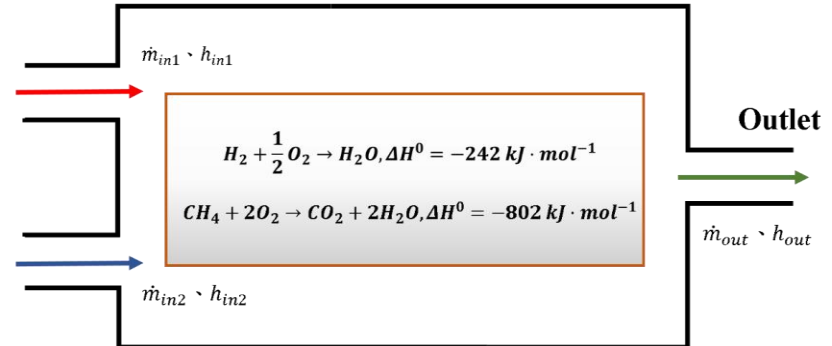
$$Z = \frac{PV}{RT}$$

- $Z$  = Compressibility factor
- $\alpha$  = Non-ideal quadratic correction parameters
- $V_m$  = molar volume of gas
- $T_c$  = Critical Temperature
- $P_c$  = Critical Pressure

## Steam Methane Reformer and Afterburner



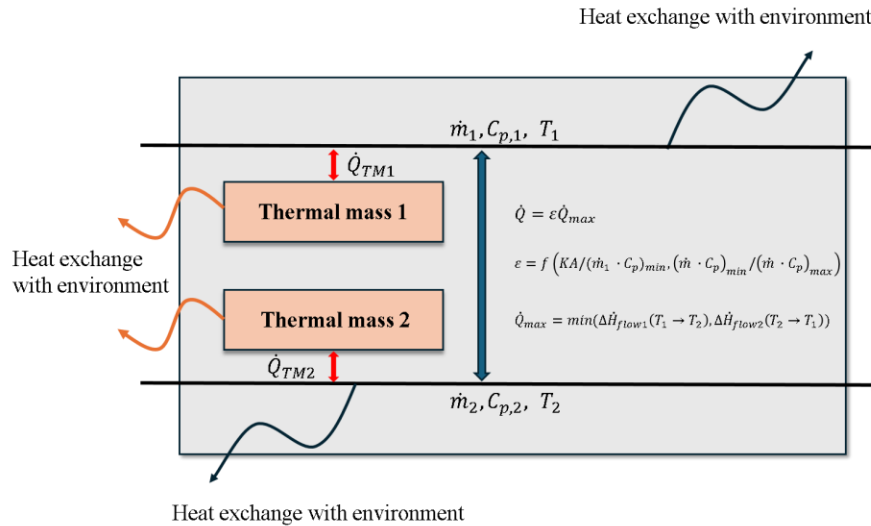
Flow 1(Anode Outlet)



Flow 2(Cathode Outlet)

# Other components

## Heater and Heat Exchanger



**Counter flow:**

$$\varepsilon = \left( \frac{1 - \exp(-N(1 - C))}{1 - C} \right)$$

$$NTU = \frac{UA}{\dot{C}_{min}}, C = \frac{\dot{C}_{min}}{\dot{C}_{max}}$$

**Solution steps:**

**Step1.**



**Step2.**



**Step3.**

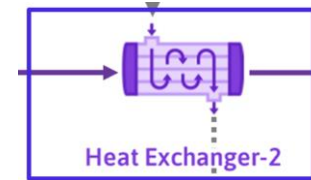
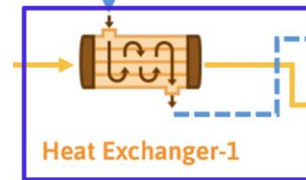


**Step4.**



**Final verification and judgment**

$$\dot{Q}_{TM,env} = \text{sign}(\dot{Q}_{env}) \times \min(|\dot{Q}_{env}|, |h_{flow}(T_i) - h_{flow}(T_{env})|)$$



$$\dot{C}_{min} = \min(\dot{m}_1 C_{p,1}, \dot{m}_2 C_{p,2})$$

$$\dot{C}_{max} = \max(\dot{m}_1 C_{p,1}, \dot{m}_2 C_{p,2})$$

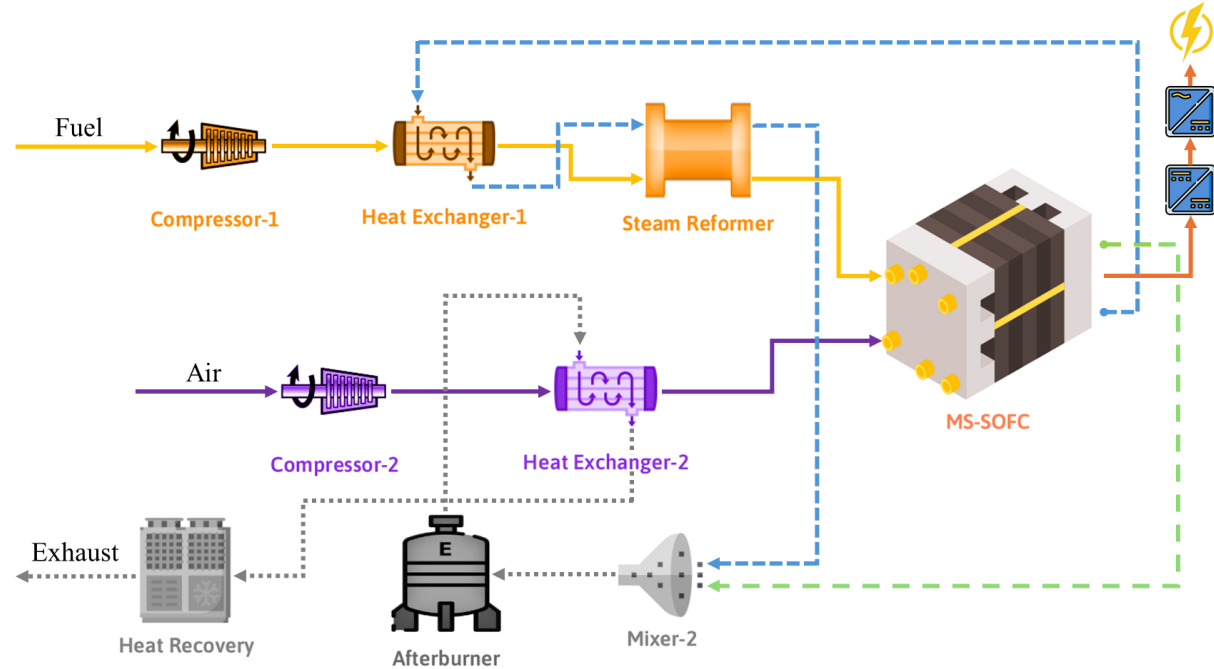
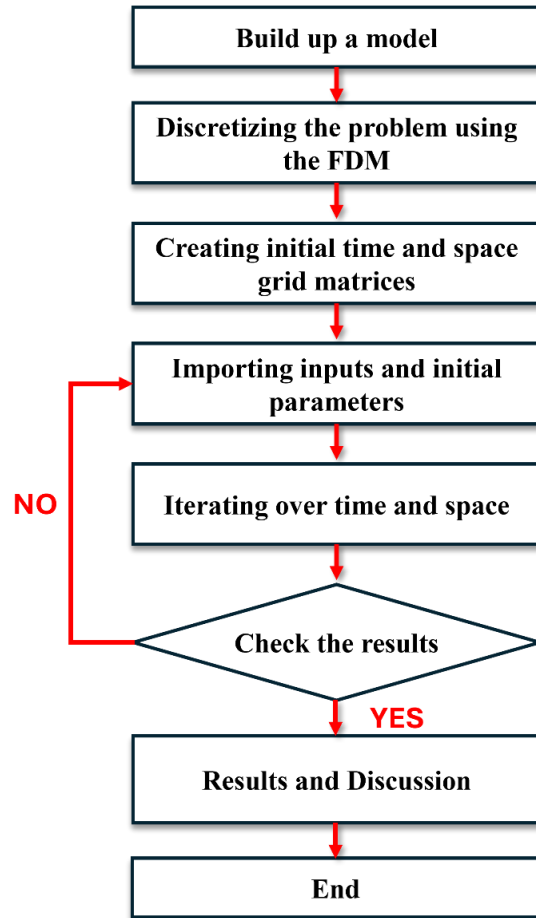
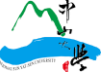
$$\dot{Q}_{max} = \dot{C}_{min} (T_{hi} - T_{ci})$$

$$\dot{Q} = \varepsilon \dot{Q}_{max}$$

$$T_{1,out} = T_{1,out} - \frac{\dot{Q}}{\dot{m}_1 C_{p,1}}$$

$$T_{2,out} = T_{2,out} - \frac{\dot{Q}}{\dot{m}_2 C_{p,2}}$$

### 3. Simulink Modeling





# Finite difference methods

## 1. Convection equation

- Mass balances of Fuel channel
- Mass balances of Air channel
- Energy balance of Fuel channel
- Energy balance of Air channel

$$\frac{\partial c_{i,f}}{\partial t} = -u_f \frac{\partial c_{i,f}}{\partial x}$$

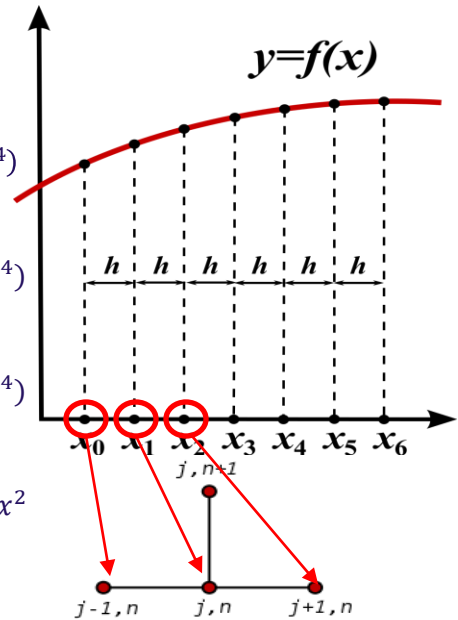
$$\frac{\partial u}{\partial t} = D \frac{\partial^2 u}{\partial x^2}$$

$$D \frac{\partial^2 u}{\partial x^2}(x_j, t_n) + f(x_j, t_n)$$

$$u(x_j, t_n + \Delta t) = u(x_j, t_n) + \frac{\partial u}{\partial t}(x_j, t_n) \Delta t + \frac{1}{2} \frac{\partial^2 u}{\partial t^2}(x_j, t_n) \Delta t^2 + \dots u(t^4)$$

$$u(x_j + \Delta x, t_n) = u(x_j, t_n) + \frac{\partial u}{\partial x}(x_j, t_n) \Delta x + \frac{1}{2} \frac{\partial^2 u}{\partial x^2}(x_j, t_n) \Delta x^2 + \dots u(x^4)$$

$$u(x_j - \Delta x, t_n) = u(x_j, t_n) - \frac{\partial u}{\partial x}(x_j, t_n) \Delta x + \frac{1}{2} \frac{\partial^2 u}{\partial x^2}(x_j, t_n) \Delta x^2 - \dots u(x^4)$$



## 2. Diffusion equation

- Energy balance of PEN structure
- Energy balance of Interconnect

$$\frac{\partial^2 u}{\partial x^2}(x_j, t_n) = [u(x_j + \Delta x, t_n) + u(x_j - \Delta x, t_n) - 2u(x_j, t_n) + \dots u(x^4)] / \Delta x^2$$



$$\frac{\partial^2 u}{\partial x^2}(x_j, t_n) \approx \frac{u_{j+1}^n - 2u_j^n + u_{j-1}^n}{\Delta x^2}$$

$$\rho_I c_{p,I} \frac{\partial T_I}{\partial t} = \lambda_I \frac{\partial^2 T_I}{\partial x^2}$$

$$u_j^{n+1} = u_j^n + \left[ D \frac{u_{j+1}^n - 2u_j^n + u_{j-1}^n}{\Delta x^2} + f_j^n \right] \Delta t$$

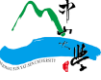
Discretization :  $x_j = x_0 + (j - 1)dx$

$$t_n = 0 + (n - 1)dt$$

$$dx = \frac{x_n - x_0}{N}$$

# Finite difference methods

## MS-SOFC

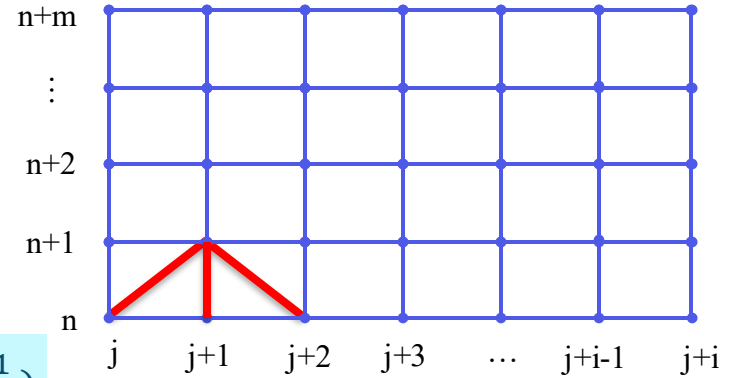


$$\frac{\partial c_{i,f}}{\partial t} = -u_f \frac{\partial c_{i,f}}{\partial x} + \sum_{k \in \{(i), (ii), (V)\}} v_{i,k} R_{i,k} \frac{1}{h_f}$$

The Concentration at the Next Time Step

$$C_{i,j}^{n+1} = C_{i,j}^n + dt * \left( -u_f \frac{C_{i,j}^n - C_{i,j-1}^n}{dx} + \sum_{k \in \{(i), (ii), (V)\}} v_{i,k} R_{i,k} \frac{1}{h_f} \right)$$

The Current Spatial Step and its Impact Factors



Finite Finite Difference approximations

$$\rho_{PEN} c_{p,PEN} \frac{\partial T_{PEN}}{\partial t} = \lambda_{PEN} \frac{\partial^2 T_{PEN}}{\partial x^2} - k_{f,PEN} (T_{PEN} - T_f) \frac{1}{\tau_{PEN}} - k_{a,PEN} (T_{PEN} - T_f) \frac{1}{\tau_{PEN}} + [(-\Delta H)_{(v)} R_{(v)} - jU] \frac{1}{\tau_{PEN}} + \left[ \frac{\sigma(T_I^4 - T_{PEN}^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_{PEN}} - 1} \right] \frac{1}{\tau_{PEN}}$$

The Temperature at the Next Time Step

$$T_{PEN,j}^{n+1} = T_{PEN,j}^n + \frac{dt}{\rho_{PEN} c_{p,PEN}} \left( \lambda_{PEN} \frac{T_{PEN,j+1}^n - 2T_{PEN,j}^n + T_{PEN,j-1}^n}{dx^2} - k_{f,PEN} (T_{PEN,j}^n - T_{f,j}) \frac{1}{\tau_{PEN}} - k_{a,PEN} (T_{PEN,j}^n - T_{f,j}) \frac{1}{\tau_{PEN}} + \dots \right)$$

The Current Spatial Step and its Impact Factors

# Model code

## 1. Parameter setting

```
% Parameter of mesh
L = 0.24;
dx = 0.04;
dt = 0.004;
x = 0:dx:L;

W       = 0.1;
h_an    = 0.001;    %fuel channel height(m)

%Molar flow Rate_anode
ndot_H2 = n_in_H2/Number_cell;
ndot_H2O = n_in_H2O/Number_cell;
ndot_CH4 = n_in_CH4/Number_cell;
ndot_CO = n_in_CO/Number_cell;
ndot_CO2 = n_in_CO2/Number_cell;
ndot_N2 = n_in_N2/Number_cell;

Pan_out = Pan;

CD       = i/(length(x)/(W*dx));
R        = 8.314;
F        = 96485;
k0       = 4274;
k_WGSR   = 0.1;
Ea       = 82;
```

## 2. Zero matrix

```
%%
% 初始化結果矩陣_anode
u1 = zeros(length(x),2);
u2 = zeros(length(x),2);
u3 = zeros(length(x),2);
u4 = zeros(length(x),2);
u5 = zeros(length(x),2);
u6 = zeros(length(x),2);

u1_2 = zeros(length(x),2);
u2_2 = zeros(length(x),2);

ndot_out_H2 = zeros(length(x),1);
ndot_out_H2O = zeros(length(x),1);
ndot_out_CH4 = zeros(length(x),1);
ndot_out_CO = zeros(length(x),1);
ndot_out_CO2 = zeros(length(x),1);
ndot_out_N2 = zeros(length(x),1);

P1 = zeros(length(x),1);
P2 = zeros(length(x),1);
P3 = zeros(length(x),1);
P4 = zeros(length(x),1);
P5 = zeros(length(x),1);
```

## 5. Calculated value output

```
ndot_out_H2(:,1) = u1(:,1)*u_an*(W*h_an)*Number_cell;
ndot_out_H2O(:,1) = u2(:,1)*u_an*(W*h_an)*Number_cell;
ndot_out_CH4(:,1) = u3(:,1)*u_an*(W*h_an)*Number_cell;
ndot_out_CO(:,1) = u4(:,1)*u_an*(W*h_an)*Number_cell;
ndot_out_CO2(:,1) = u5(:,1)*u_an*(W*h_an)*Number_cell;
ndot_out_N2(:,1) = u6(:,1)*u_an*(W*h_an)*Number_cell;

n_out_H2 = ndot_out_H2(end,1);
n_out_H2O = ndot_out_H2O(end,1);
n_out_CH4 = ndot_out_CH4(end,1);
n_out_CO = ndot_out_CO(end,1);
n_out_CO2 = ndot_out_CO2(end,1);
n_out_N2 = ndot_out_N2(end,1);
```

## 3. Initial value setting

```
%Concentration calculation_anode
C1 = (Pan*ndot_H2)/(8.2057e-5*T_an_in*(ndot_H2+ndot_H2O+ndot_CH4+ndot_CO+ndot_CO2));
C2 = (Pan*ndot_H2O)/(8.2057e-5*T_an_in*(ndot_H2+ndot_H2O+ndot_CH4+ndot_CO+ndot_CO2));
C3 = (Pan*ndot_CH4)/(8.2057e-5*T_an_in*(ndot_H2+ndot_H2O+ndot_CH4+ndot_CO+ndot_CO2));
C4 = (Pan*ndot_CO)/(8.2057e-5*T_an_in*(ndot_H2+ndot_H2O+ndot_CH4+ndot_CO+ndot_CO2));
C5 = (Pan*ndot_CO2)/(8.2057e-5*T_an_in*(ndot_H2+ndot_H2O+ndot_CH4+ndot_CO+ndot_CO2));
C6 = (Pan*ndot_N2)/(8.2057e-5*T_an_in*(ndot_H2+ndot_H2O+ndot_CH4+ndot_CO+ndot_CO2));

u_an = (ndot_H2+ndot_H2O+ndot_CH4+ndot_CO+ndot_CO2)/((C1+C2+C3+C4+C5)*(W*h_an));

%%

matrix_H2 = (Pan*matrix_in_H2)/(8.2057e-5*T_an_x.*(matrix_in_H2+matrix_in_H2O+matrix_in_CH4+matrix_in_CO+matrix_in_CO2+matrix_in_N2));
matrix_H2O = (Pan*matrix_in_H2O)/(8.2057e-5*T_an_x.*(matrix_in_H2+matrix_in_H2O+matrix_in_CH4+matrix_in_CO+matrix_in_CO2+matrix_in_N2));
matrix_CH4 = (Pan*matrix_in_CH4)/(8.2057e-5*T_an_x.*(matrix_in_H2+matrix_in_H2O+matrix_in_CH4+matrix_in_CO+matrix_in_CO2+matrix_in_N2));
matrix_CO = (Pan*matrix_in_CO)/(8.2057e-5*T_an_x.*(matrix_in_H2+matrix_in_H2O+matrix_in_CH4+matrix_in_CO+matrix_in_CO2+matrix_in_N2));
matrix_CO2 = (Pan*matrix_in_CO2)/(8.2057e-5*T_an_x.*(matrix_in_H2+matrix_in_H2O+matrix_in_CH4+matrix_in_CO+matrix_in_CO2+matrix_in_N2));
matrix_N2 = (Pan*matrix_in_N2)/(8.2057e-5*T_an_x.*(matrix_in_H2+matrix_in_H2O+matrix_in_CH4+matrix_in_CO+matrix_in_CO2+matrix_in_N2));

%The input matrix from the previous time step
u1(:,1) = matrix_H2;
u2(:,1) = matrix_H2O;
u3(:,1) = matrix_CH4;
u4(:,1) = matrix_CO;
u5(:,1) = matrix_CO2;
u6(:,1) = matrix_N2;

%Boundary_H2_H2O_CH4_CO_CO2
u1(1,1) = C1;
u2(1,1) = C2;
u3(1,1) = C3;
u4(1,1) = C4;
u5(1,1) = C5;
u6(1,1) = C6;
```

## 4. Calculate value iteration

```
for n = 1
    for j = 1:length(x)-1

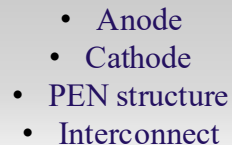
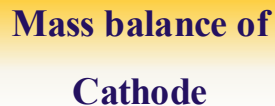
        f1(f1 < 0 | isnan(f1)) = 0;
        f2(f2 < 0 | isnan(f2)) = 0;
        f3(f3 < 0 | isnan(f3)) = 0;

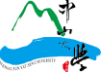
        u1(j+1,n+1) = u1(j+1,n) - ((dt*u_an/dx)*(u1(j+1,n) - u1(j,n)))+dt/h_an*(+3*f2(j+1,n)+1*f3(j+1,n));
        u2(j+1,n+1) = u2(j+1,n) - ((dt*u_an/dx)*(u2(j+1,n) - u2(j,n)))+dt/h_an*(-1*f2(j+1,n)-1*f3(j+1,n));
        u3(j+1,n+1) = u3(j+1,n) - ((dt*u_an/dx)*(u3(j+1,n) - u3(j,n)))+dt/h_an*(-1*f2(j+1,n)+0*f3(j+1,n));
        u4(j+1,n+1) = u4(j+1,n) - ((dt*u_an/dx)*(u4(j+1,n) - u4(j,n)))+dt/h_an*(+1*f2(j+1,n)-1*f3(j+1,n));
        u5(j+1,n+1) = u5(j+1,n) - ((dt*u_an/dx)*(u5(j+1,n) - u5(j,n)))+dt/h_an*(+0*f2(j+1,n)+1*f3(j+1,n));
        u6(j+1,n+1) = u6(j+1,n) - ((dt*u_an/dx)*(u6(j+1,n) - u6(j,n)))+dt/h_an*(+0*f2(j+1,n)+0*f3(j+1,n));

        u1_2(j+1,n+1) = u1(j+1,n+1)+dt/h_an*(-1*f1(j+1,n));
        u2_2(j+1,n+1) = u2(j+1,n+1)+dt/h_an*(+1*f1(j+1,n));

        if u1(j+1,n+1)<=0
            f1(j+1,n)=0;
        else
            f1(j+1,n)=f1(j+1,n);
        end
    end
end
```

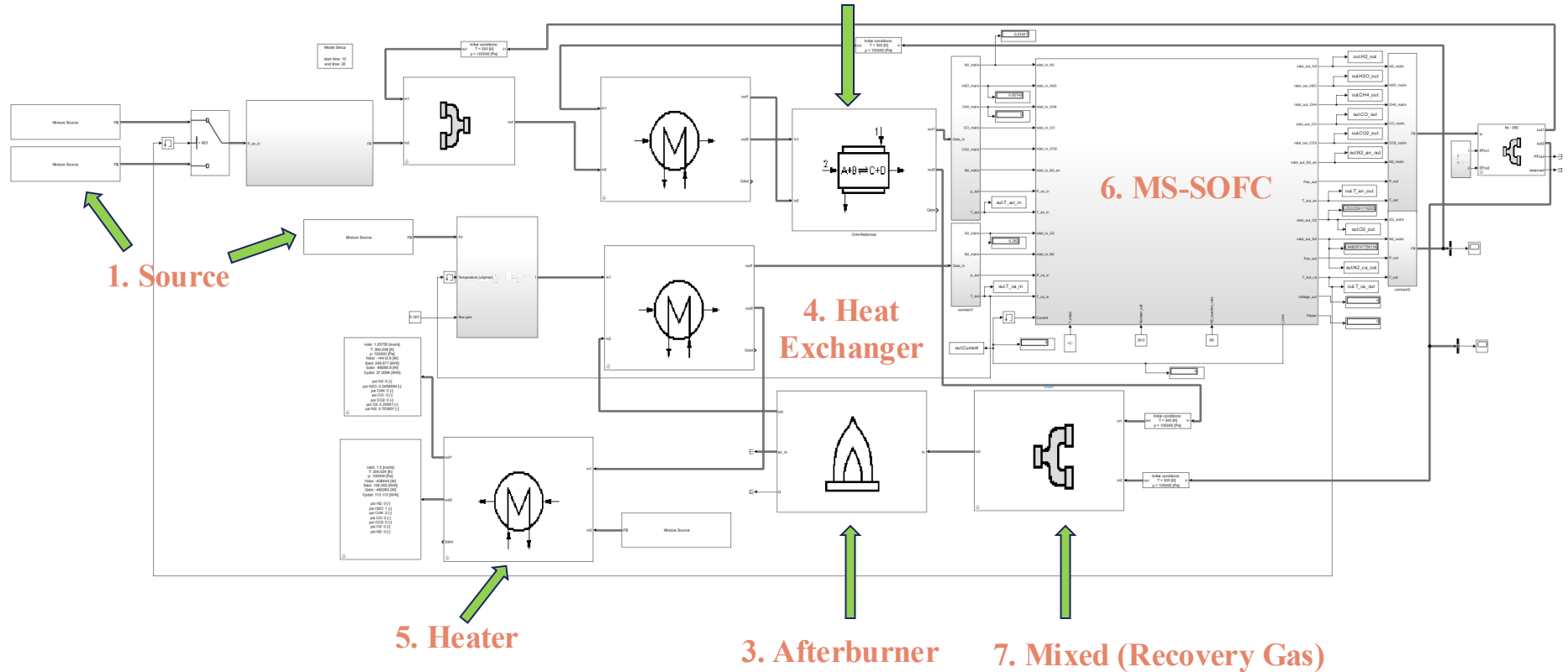






# MS-SOFC system assembly

## 2. Steam Methane Reformer



# Anode-Supported SOFC (Verification)

Table 1. Structural parameters of AS-SOFC

Structural parameters of AS-SOFC	
Cell length, L	0.4 m
Cell length, W	0.1 m
Fuel channel height, $h_a$	1 mm
Air channel height, $h_f$	1 mm
Anode thickness, $\tau_{anode}$	500 $\mu\text{m}$
Cathode thickness, $\tau_{cathode}$	50 $\mu\text{m}$
Electrolyte thickness, $\tau_{electrolyte}$	200 $\mu\text{m}$
Interconnect thickness, $\tau_I$	500 $\mu\text{m}$

Table 2. Operating Conditions of AS-SOFC

Operating Conditions of AS-SOFC	
Pressure of anode, $P_{an}$	1.3 bar
Pressure of anode, $P_{ca}$	1.1 bar
Fuel inlet temperature, $T_f^0$	973 K
Air inlet temperature, $T_a^0$	973 K
Air feed	21% O <sub>2</sub> , 79% N <sub>2</sub>
Air ratio, $\lambda_{air}$	8.5

Table 3. Physical properties and material parameters of AS-SOFC

Physical properties and material parameters of AS-SOFC	
Anode electrical conductivity, $\sigma_{anode}$	$80 \times 10^3 \Omega^{-1}\text{m}^{-1}$
Cathode electrical conductivity, $\sigma_{ca}$	$8.4 \times 10^3 \Omega^{-1}\text{m}^{-1}$
PEN density, $\rho_{PEN}$	5900 kg m <sup>-3</sup>
PEN heat capacity, $c_{p,PEN}$	0.5 kJ kg <sup>-1</sup> K <sup>-1</sup>
PEN thermal conductivity, $\lambda_{PEN}$	$2 \times 10^{-3} \text{ kJ m}^{-1}\text{s}^{-1}\text{K}^{-1}$
PEN emissivity, $\epsilon_{PEN}$	0.8
Electrolyte ionic conductivity, $\lambda_{electrolyte}$	$33.4 \times 10^3 \exp(-10.3 \times 10^3 / T) \Omega^{-1}\text{m}^{-1}$
Interconnect density, $\rho_I$	8000 kg m <sup>-3</sup>
Interconnect heat capacity, $c_{p,I}$	0.5 kJ kg <sup>-1</sup> K <sup>-1</sup>
Interconnect thermal conductivity, $\lambda_I$	$25 \times 10^{-3} \text{ kJ m}^{-1} \text{ s}^{-1}\text{K}^{-1}$
Interconnect emissivity, $\epsilon_I$	0.1
Anode diffusion coefficient, $D_{eff,anode}$	$3.66 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$
Cathode diffusion coefficient, $D_{eff,cathode}$	$1.37 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$

Ref. Aguiar, Patricia, Claire S. Adjiman, and Nigel P. Brandon. "Anode-supported intermediate temperature direct internal reforming solid oxide fuel cell. I: model-based steady-state performance." *Journal of power sources* 138.1-2 (2004): 120-136.

# Mesh validation

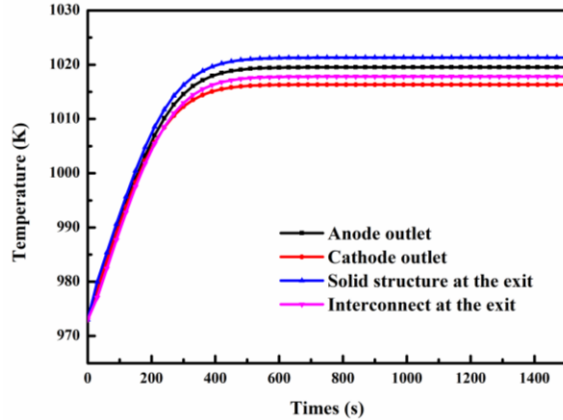


Fig1. The temperature at the outlet of each area at different time points

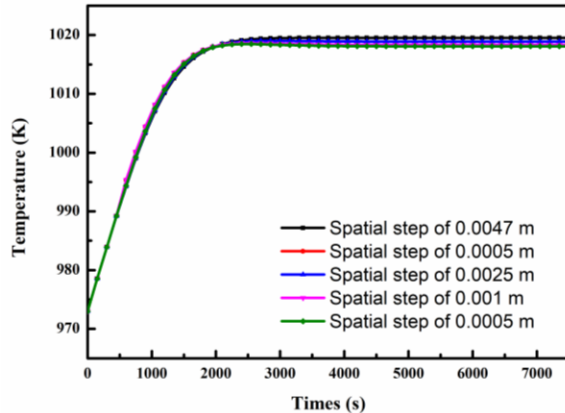


Fig2. Comparison chart of anode outlet temperature results at different spatial steps at different times

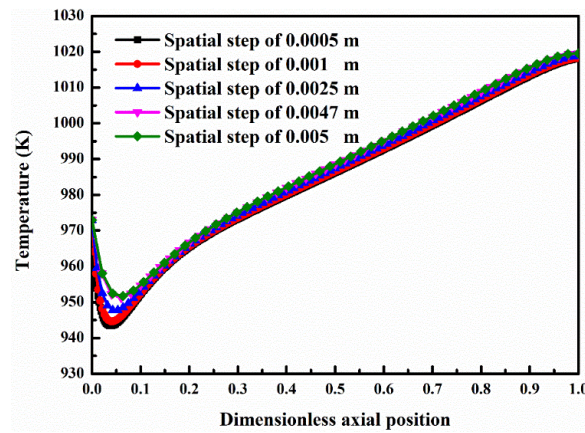
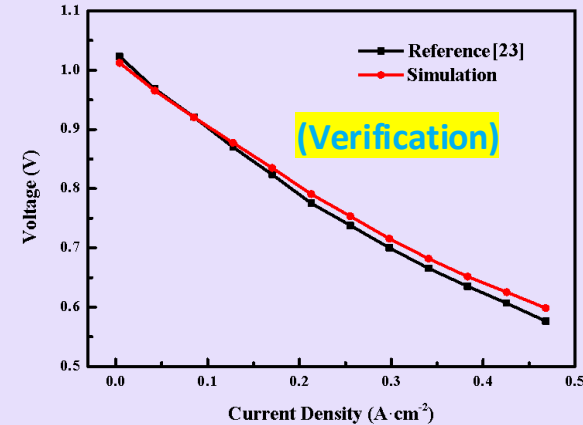


Fig3. Comparison of the Impact of Different Spatial Step Sizes on the Numerical Simulation Results of Temperature Distribution in the Anode Flow Channel

## Model validation

Fig.4. Comparison of simulated voltage response with experimental response reported in [23].



[23] Ref. Aguiar, Patricia, Claire S. Adjiman, and Nigel P. Brandon. "Anode-supported intermediate temperature direct internal reforming solid oxide fuel cell. I: model-based steady-state performance." *Journal of power sources* 138.1-2 (2004): 120-136.

Table6. Operating Conditions of MS-SOFC (Data1)

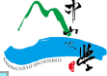
Operating Conditions of MS-SOFC (Data1)	
Pressure of anode, $P_{an}$	1.3 bar
Pressure of anode, $P_{ca}$	1.1 bar
Fuel inlet temperature, $T_f^0$	973 K
Air inlet temperature, $T_a^0$	973 K
Air feed	21% O <sub>2</sub> , 79% N <sub>2</sub>
Air flow velocity	3.6 m s <sup>-1</sup>
Fuel feed	100% H <sub>2</sub>
fuel flow velocity	0.6 m s <sup>-1</sup>

Table7. Operating Conditions of MS-SOFC (Data2)

Operating Conditions of MS-SOFC (Data2)	
Pressure of anode, $P_{an}$	1.3 bar
Pressure of anode, $P_{ca}$	1.1 bar
Fuel inlet temperature, $T_f^0$	873 K
Air inlet temperature, $T_a^0$	873 K
Air feed	21% O <sub>2</sub> , 79% N <sub>2</sub>
Air flow velocity	3.6 m s <sup>-1</sup>

Fuel flow rate, gas composition, water-to-carbon ratio, and reforming reaction rate of MS-SOFC.

Pure hydrogen fuel				
0.104 mol s <sup>-1</sup>		100 % H <sub>2</sub>		
Mixed fuel				
0.045 mol s <sup>-1</sup> H <sub>2</sub> , Water to carbon ratio (S/C) H <sub>2</sub> O, 0.015 mol s <sup>-1</sup> CH <sub>4</sub> , 0.007 mol s <sup>-1</sup> CO, 0.047 mol s <sup>-1</sup> CO <sub>2</sub>				
		Steam reforming rate		
S/C 2 (S/C: Water to carbon ratio)		50 %	75 %	100%
S/C 2.5		50 %	75 %	100%
S/C 3		50 %	75 %	100%
Pure Methane fuel				
Water to carbon ratio (S/C) H <sub>2</sub> O, 0.026 mol s <sup>-1</sup> CH <sub>4</sub>				
	Steam reforming rate			
S/C 2	25%	50 %	75 %	100%
S/C 2.5	25%	50 %	75 %	100%
S/C 3	25%	50 %	75 %	100%



## Data1. Model validation

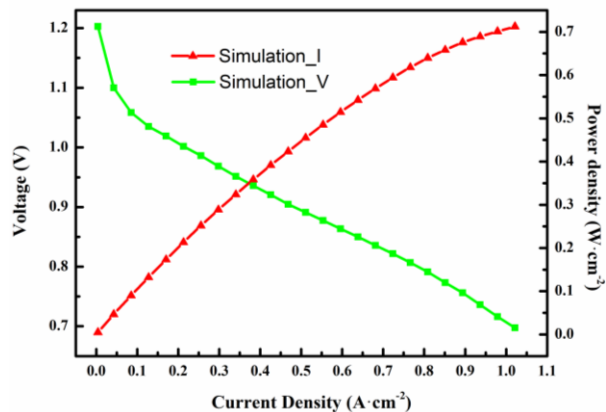


Fig5. Pure hydrogen fuel current density curve

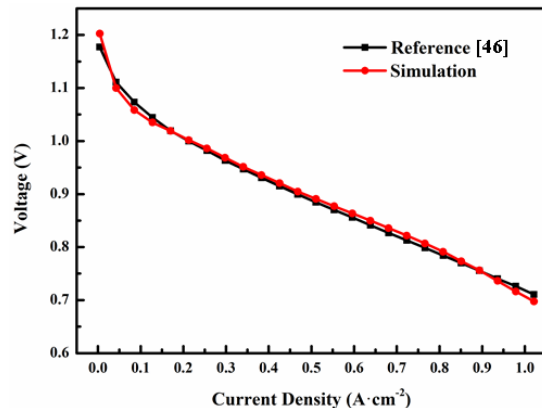


Fig6. Comparison chart of the relationship between voltage, current density and reference value

## Data2. Steady state performance analysis

Pure hydrogen fuel,  $0.104 \text{ mol s}^{-1} \text{ H}_2$

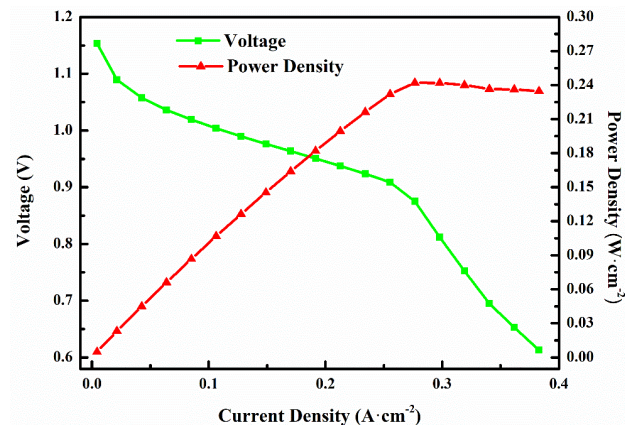


Fig.7. Simulation results for voltage vs. power density characteristics of MS-SOFC with

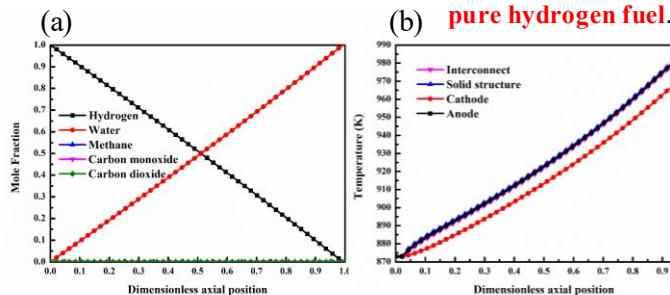


Fig.8. Distribution of hydrogen mole fraction in anode flow channel under peak power density conditions with **pure hydrogen fuel.**

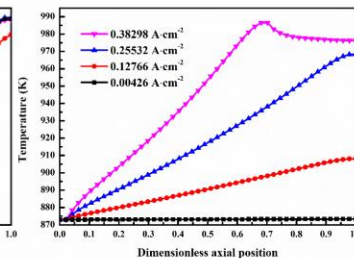
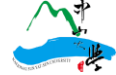
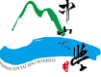


Fig.9. Temperature distribution in anode channel of MS-SOFC with different current densities





# Conclusion



The designed model incorporates mass and energy balance equations, as well as electrochemical models. Simulations have been performed to investigate the electrochemical behavior of the MS-SOFC, the temperature distribution within the multi-layer SOFC structure, and the fuel component fractions at the inlet and outlet of the anode channel under the effects of different water-to-carbon ratios ( $S/C = 2, 2.5, \text{ and } 3$ ) and methane vapor refining reaction rates (50%, 75%, and 100%). Two fuels have been considered: pure hydrogen and a mixed fuel containing hydrogen, methane, carbon monoxide, and carbon dioxide. The simulations have focused on the problem of maximizing the current density in the MS-SOFC while simultaneously maintaining a low operating temperature of  $600^{\circ}\text{C}$  by controlling the  $S/C$  ratio and methane vapor refining reaction rate. **Peak power density (PPD)** under different conditions:

Input conditions	Pure hydrogen fuel	Mixed fuel, $S/C=2$			Mixed fuel, $S/C=2.5$			Mixed fuel, $S/C=3$		
		SMR50%	SMR75%	SMR100%	SMR50%	SMR75%	SMR100%	SMR50%	SMR75%	SMR100%
PPD value	0.24201	0.17889	0.21004	0.23041	0.17422	0.20873	0.22882	0.17271	0.20760	0.22734

Pure methane fuel, $S/C=2$				Pure methane fuel, $S/C=2.5$				Pure methane fuel, $S/C=3$			
SMR25%	SMR50%	SMR75%	SMR100%	SMR25%	SMR50%	SMR75%	SMR100%	SMR25%	SMR50%	SMR75%	SMR100%
0.03255	0.07520	0.12415	0.16381	0.03339	0.07873	0.13018	0.17043	0.03435	0.08007	0.13316	0.17808

➤ **PPD: Peak Power Density**   ➤ **SMRR: Steam Methane reforming rate**   ➤  **$S/C$ : Water to carbon ratio**

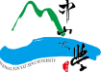
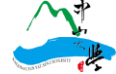


Table 7. Coefficients used to calculate specific heat capacity of MS-SOFC.

	H <sub>2</sub>	H <sub>2</sub> O	CH <sub>4</sub>	CO	CO <sub>2</sub>	O <sub>2</sub>	N <sub>2</sub>
B	2.47906	4.00392	4.00088	3.50055	3.50002	3.50146	3.50031
C	0.95806	0.01059	0.76315	1.02865	2.04452	1.07558	0.13732
D	228.734	268.795	820.659	1550.45	919.306	2235.71	662.738
E	0.45444	0.98763	0.0046	0.00493	-1.06044	1.01334	-0.1466
F	326.843	1141.41	178.41	704.525	865.07	1116.69	680.562
G	1.56039	3.06904	8.74432	0	2.03366	0	0.90066
H	1651.71	2507.37	1.062.82	0	483.553	0	1740.060
I	-1.376	0	-4.469	0	0.014	0	0
J	1671.69	0	1090.53	0	341.109	0	0
M	2.016	18.015	16.043	28.01	44.01	31.999	28.013

The specific heat capacity of MS-SOFC,  $c_p$ , is defined using data from ISO 20765-1 [25]. Based on this data, **we derived a novel ideal gas temperature polynomial equation**, referred to as the **Kuo and Liu equation**, to determine the **specific heat capacity ( $C_{pi}^0$ ) of MS-SOFC**. The coefficients for this equation are provided in Table 7.

$$\frac{C_{pi}^0}{R/M} = B + C \left( \frac{D/T}{\sinh(D/T)} \right)^2 + E \left( \frac{F/T}{\cosh(F/T)} \right)^2 + G \left( \frac{H/T}{\sinh(H/T)} \right)^2 + I \left( \frac{J/T}{\cosh(J/T)} \right)^2$$



➤ **Four value chains representing opportunities for scaling up Hydrogen in the near term**

1. **To open gateways to lower-cost and lower-carbon hydrogen hubs.**  
✓ Europe, United States, Japan, Middle East , Latin America, Taiwan, China, Australia
2. **To Scale up low-carbon hydrogen supply by tapping into dependable demand.**  
✓ North America, Europe, Middle East
3. **To reach the appropriate scale for competitive fuel cell vehicles and refueling.**  
✓ Japan, Korea, China, Europe, United States
4. **To kick-start international hydrogen trade for the ultimate global low-carbon market.**  
✓ Asia Pacific, Middle East, North Africa, Europe



- **Wider Hydrogen Value Chain Risks and Dependencies**
  - ✓ Blue and green hydrogen **competition**
  - ✓ Markets and regulations, **safety and public trust**
  - ✓ **Skills** gaps
  - ✓ **Resource efficiency** and embodied carbon in infrastructure
  - ✓ The atmospheric **greenhouse effect of hydrogen leakages**
  - ✓ Global production and use of **hydrogen and international trade**
  - ✓ **Cost uncertainties** of imports
  - ✓ **Emission uncertainties** of hydrogen imports

# 2025 H2 Energy and Fuel cell Conference



# Laboratory Team Members



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